

Signals and Communication Technology

Behrouz Zolfaghari  
Khodakhast Bibak

# Perfect Secrecy in IoT

A Hybrid Combinatorial-Boolean  
Approach

 Springer

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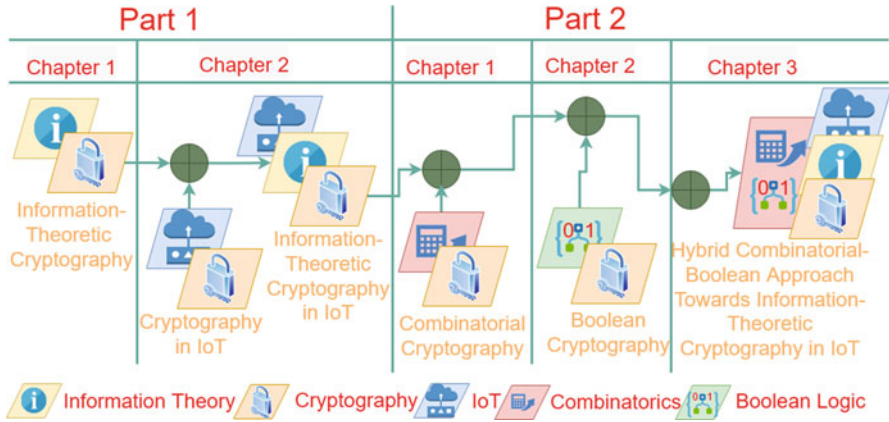
*I would like to dedicate this book to my  
beloved wife Saeideh for all her patience and  
her kind support.*

# Preface

Perfectly secure cryptography is a branch of information-theoretic cryptography. A perfectly secure cryptosystem guarantees that the malicious third party cannot guess anything regarding the plain text or the key, even in the case of full access to the cipher text. Despite this advantage, there are only a few real-world implementations of perfect secrecy due to some well-known limitations. Any simple, straightforward modeling can pave the way for further advancements in the implementation, especially in environments with time and resource constraints such as IoT. This book takes one step towards this goal via presenting a hybrid combinatorial-Boolean model for perfectly secure cryptography in IoT.

In this book, we first present an introduction to information-theoretic cryptography as well as perfect secrecy and its real-world implementations. Then we take a systematic approach to highlight information-theoretic cryptography as a convergence point for existing trends in research on cryptography in IoT. Then we investigate combinatorial and Boolean cryptography and show how they are seen almost everywhere in the ecosystem and the life cycle of information-theoretic IoT cryptography. We finally model perfect secrecy in IoT using Boolean functions, and map the Boolean functions to simple, well-studied combinatorial designs like Latin squares.

This book is organized in two parts. The first part studies information-theoretic cryptography and the promise it holds for cryptography in IoT. The second part separately discusses combinatorial and Boolean cryptography, and then presents



**Fig. 1** The organization of the book along with the purpose of each part and each chapter

the hybrid combinatorial-Boolean model for perfect secrecy in IoT. Figure 1 illustrates the organization of this book along with the purpose of each part and each chapter.

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# Part I

## Information-Theoretic Cryptography and Perfect Secrecy

This part consists of two chapters. The first chapter presents an overview on information-theoretic and perfectly secure cryptography and studies one-time pad (OTP) as the only real-world implementation of perfect secrecy.

In the second chapter, we first study the trade-offs between the real-time requirements of cryptography in IoT systems and the resource constraints in these environments. Then, we show how these trade-offs can be resolved using information-theoretic cryptography. We highlight information-theoretic cryptography as the convergence point of research on real-time cryptography and resource-constrained cryptography in IoT.

# Chapter 1

## Information-Theoretic Cryptography and Perfect Secrecy



### 1.1 Introduction

Information theory is about measuring, storing, and transmitting digital information. The foundation of this discipline was historically built by Nyquist and Hartley in the 1920s and later by Shannon in the 1940s. Information theory is supported by statistics, statistical mechanics, probability theory, information engineering, electrical engineering, and computer science. In this chapter, we present an overview on the applications of information theory and related concepts in cryptography. We specifically focus on perfectly secure cryptography, which is a well-studied branch of information-theoretic cryptography. Our proposed approach for cryptography in IoT (to be introduced later in this book) is aimed to provide perfect secrecy.

The rest of this chapter is organized as follows: Sect. 1.2 introduces entropy as the central concept in information theory. This section studies the path of entropy from thermodynamics through information technology into cryptography. Section 1.3 sheds light on the role of entropy and information theory in the ecosystem of cryptography. Section 1.4 discusses perfect secrecy as a well-studied branch of information-theoretic cryptography. Different notions and variants of perfect secrecy are studied in this section. Moreover, different approaches to the implementation of perfect secrecy are reviewed in this section. The discussions of this section are important as this book proposes an approach toward perfect secrecy in IoT. Section 1.5 is about one-time pad (OTP) cryptography, the only real-world implementation of perfect secrecy. In this section, we study the whole ecosystem of OTP and discuss the role of OTP in the future of cryptography.

## 1.2 Entropy: From Thermodynamics to Information Theory

The term *entropy* has its roots in statistical mechanics and thermodynamics, where the internal disorder of a system in a given macroscopic state is stated as a logarithmic function of the number  $\Omega$  of possible microscopic system configurations. Such a definition is given in Eq. (1.1).

$$S = k_B \ln \Omega. \quad (1.1)$$

In Eq. (1.1),  $S$  represents the entropy, and  $k_B$  is referred to as *Boltzmann constant*. Obviously, under equiprobability assumptions,  $\Omega$  will be an exponential function of the number of particles able to randomly move within the system. Put alternatively,  $\ln \Omega$  is proportional to the number of random particles inside the system, which is a measure of randomness. This number is converted to the total uncontrolled kinetic energy of the random particles by Boltzmann constant. Moreover, the number of randomly moving particles inside a system is a representative of the amount of information needed to define the exact state of a system given its macroscopic state. As suggested by the above discussions, the thermodynamic concept of entropy connects the uncontrolled internal energy of a system to randomness, disorder, and unavailable information.

Information entropy (information-theoretical entropy) was first introduced by Shannon [1, 2] working on cryptographic projects in World War. This entropy can be assigned to a random variable as the average level of *self-information* in each possible event of the variable, which represents the inherent level of uncertainty or surprise in the event. For a random variable  $X$ , Shannon defined the self-information  $I_X$  of an event  $x_i$  with probability  $P_X(x_i)$  as shown by Eq. (1.2).

$$I_X(x_i) = -\log_b P_X(x_i). \quad (1.2)$$

In Eq. (1.2), the unit of information is determined by the base  $b$ . Especially, if  $b = 2$ ,  $I_X(x_i)$  is calculated in bits. In Shannon's theory, the entropy  $H$  of  $X$  is defined by Eq. (1.3),

$$H(X) = E[I_X] = \sum_i P_X(x_i) I_X(x_i) = -\sum_i P_X(x_i) \log_b P_X(x_i). \quad (1.3)$$

In Eq. (1.3),  $E[I_X]$  is the mathematical expectation of  $I_X$ . Von Neumann suggested the name "entropy" for the concept introduced by Shannon because of the similarity of its notion and formulation to those of thermodynamic entropy. In fact, both information-theoretic and thermodynamic entropy are used as measures of unavailable information, disorder, and randomness. Shannon discussed the role of entropy and related concepts in the modeling of cryptosystems. Further, he introduced the notion of perfectly secure cryptosystem on the basis of entropy.

Different notions of information entropy have been suggested by different researchers. In the rest of this book, the term “entropy” refers to information-theoretic entropy, unless we clearly specify thermodynamic entropy.

### 1.3 Information Theory: Everywhere in the Ecosystem of Cryptography

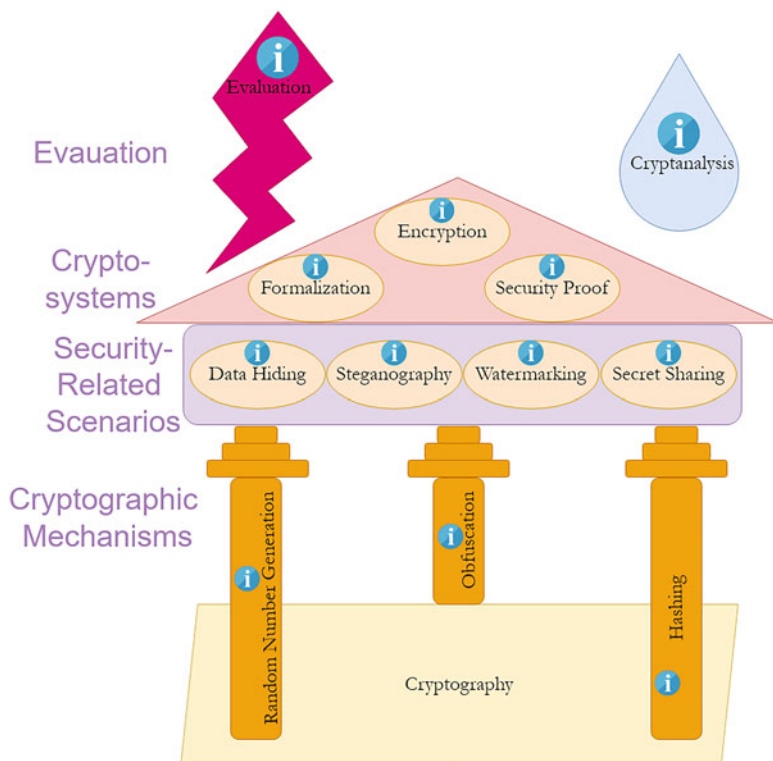
Entropy has found its applications in a variety of scientific and technological areas [3–5]. Many research reports have addressed the role of entropy in the design, implementation, and analysis of cryptosystems as well as cryptographic applications and environments [6]. Several survey reports have reviewed the applications of entropy in a variety of areas, such as economics [7], image processing [8], discrete mathematics [9], signal processing [10], etc.

Recent research connects different aspects of cryptosystems to entropy. Maurer has investigated the role of entropy in the calculation of the lower bounds on key size, and studied the relation between entropy and perfect secrecy [11]. As another example, a quick overview on some entropy-related notions and their applications in cryptosystems has been presented by Reyzin [12]. Moreover, the relation between entropy and true randomness as well as key unpredictability has been investigated by Vassilev and Hall [13]. In the following, we study some cryptographic applications of entropy and information theory.

More generally, information theory has many applications in cryptography and cryptology, among which one may refer to the following:

- Applications in cryptosystems  
Information theory has been used in the design of encryption algorithms as formalization and security proof of cryptosystems [14, 15].
- Applications in evaluation and cryptanalysis [16–18]
- Applications in cryptographic mechanisms  
Recent literature highlights the applications of information theory in a variety of cryptographic mechanisms. To mention a few, we can refer to the following:
  - Obfuscation [19, 20]
  - Hashing [21–23]
  - Random number generation [24]
- Applications in security-related scenarios  
In addition to direct applications in cryptography, information theory has found its applications in several related areas. Some of these areas are mentioned below:
  - Data hiding [25, 26]
  - Steganography and steganalysis [27, 28]
  - Watermarking [29]
  - Secret sharing [30–33]





**Fig. 1.1** The ecosystem of cryptography and the role of information theory

The above discussions highlight the role of information theory in the ecosystem of cryptography, which includes encryption and evaluation, cryptographic mechanisms, and related areas. This role can be seen in Fig. 1.1.

## 1.4 Perfect Secrecy

Perfect secrecy is a branch of information-theoretic security. A cryptosystem is perfectly secure if an adversary's knowledge of the contents of the plain text is the same both before and after they get unlimited access to the cipher text, inspecting it via all possible attack approaches with unlimited resources. As a very simple example, suppose the 1-bit cipher  $\mathcal{C}(P, K) = P \oplus K$  defined by the truth table shown in Table 1.1.

$\mathcal{C}$  is perfectly secure as, whether the cipher text is 0 or 1, the plain text can be 0 or 1 both with identical probabilities.

**Table 1.1** A 1-bit perfectly secure cipher

$P$	$K$	$C(P, K) = P \oplus K$
0	0	0
0	1	1
1	0	1
1	1	0

### 1.4.1 Notions

Different notions of perfect secrecy have been used in research on cryptography. To mention a few, one may refer to the following notions:

- Shannon notion[34, 35]  
As defined by Shannon, perfect secrecy holds if  $H(P|C) = H(P)$  and  $H(K|C) = H(K)$ , where  $P$ ,  $K$ , and  $C$  are the plain text, the key, and the cipher text, respectively, and  $H(P|C)$  and  $H(K|C)$  are the conditional entropies of the plain text and the key given the cipher text. We use this notion in our approach in the last chapter of this book.
- Mutual information notion[36]
- Perfect omniscience notion[37]
- Large-deviations notion[38]

### 1.4.2 Approaches

Different approaches have been taken toward achieving perfect secrecy. Among these approaches, we can mention jamming [39] or compressed sensing [40]. However, combinatorial approaches [41, 42] are the most relevant to our discussions in this book.

### 1.4.3 Variants

In addition to different notions and different approaches, researchers have proposed and applied different variants of perfect secrecy. Some of these variants are as follows:

- Relative perfect secrecy [43]
- Asymptotic perfect secrecy [44]

### ***1.4.4 Applications in Cryptography***

The literature comes with several applications of perfect secrecy in cryptography [45–47]. Some aspects of these applications are mentioned below.

#### **1.4.4.1 Application on Different Content Types**

Perfectly secure encryption has been applied on a variety of content types ranging from analog signals [48] to individual sequences [49].

#### **1.4.4.2 Applications in Cryptography-Related Areas**

Different cryptography-related areas can take advantage of perfect secrecy, with different notions, via different approaches. In the following, we mention some of these areas:

- Data hiding [50, 51]
- Authentication [52]

#### **1.4.4.3 Applications in Coding and Communication**

Applications of perfect secrecy are not limited to cryptography and cryptography-related areas. Some other communications are as follows:

- Applications in coding  
There are a variety of perfectly secure codes and coding schemes, some of which are listed below:
  - Perfectly secure error-free coding [53]
  - Perfectly secure network coding [54, 55]
  - Index coding [56, 57]
  - Storage coding [58]
  - Perfectly secure coded caching [59]
  - Other perfectly secure codes [60]
- Applications in communication [61–63]

#### **1.4.4.4 Technological Applications**

As suggested by recent research works, perfectly secure cryptography can serve to the security of different computing environments, some of which are mentioned below:

- Unmanned aerial vehicles (UAVs)  
Avdonin et al. [64] A method of creating perfectly secure data transmission channel between unmanned aerial vehicle and ground control station based on one-time pads 2017
- Wireless sensor networks (WSNs) [65]
- Mobile networks [66]
- Cloud computing environments [67]
- Internet of Things (IoT)[68]

## 1.5 One-Time Pad (OTP): The Only Real-World Implementation

Despite its advantages, perfect secrecy is hard to implement. The reason is that a perfectly secure cryptosystem requires the key to be of identical length with the plain text.

OTP is the only real-world implementation of perfectly secure cryptography. In recent years, OTP has been of interest to the cryptography research community [69, 70]. It has been proven to be a suitable choice for different cryptographic scenarios including the following:

- On-the-fly encryption [71]
- Lightweight encryption [72]
- Instant messaging [73]

Figure 1.2 shows how OTP works.

Figure 1.3 shows the relation among information-theoretic security, perfect secrecy, and OTP.

In the following, we take a look at the ecosystem and the future of OTP cryptography.

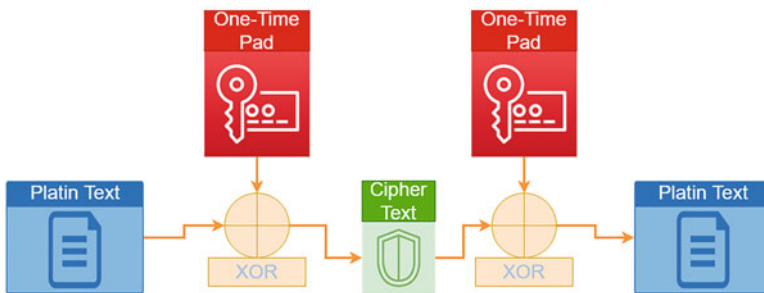
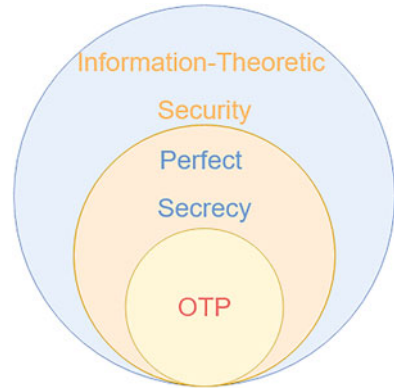


Fig. 1.2 One-time pad cipher

**Fig. 1.3** Perfect secrecy as a branch of information-theoretic security and OTP as the only real-world implementation of perfect secrecy



### 1.5.1 The Ecosystem of OTP Cryptography

In the following, we study the ecosystem of OTP, consisting of the enablers, the applications, and the challenges. By enablers, we mean the sciences and technologies that support the design, implementation, and evaluation of an OTP system.

#### 1.5.1.1 Enablers

Different technologies and branches of science have been used to support OTP cryptosystems. Among these enablers, one may refer to the following:

- True random number generation (TRNG) [74]
- Logical operations [75]
- Traditional ciphers [76–78]

#### 1.5.1.2 Applications

The applications of OTP cryptography can be divided into the following two categories:

- Applications in security-related scenarios  
Several cryptography-related areas can take advantage of OTP cryptography. Some of these areas are as follows:
  - Authentication [79, 80]
  - Watermarking [81]
  - Steganography [82]

- Applications in technological fields  
Among potential technological applications of OTP, one may refer to the following:
  - Health and medical technology [83, 84]
  - Communication systems [85]
  - Coding systems [59, 86]
  - Financial technology (FinTech) [87]
  - Cloud computing [88]
  - IoT (Internet of Things) [89]
  - Aerospace technology [90]

### 1.5.1.3 Challenges

As suggested by recent research works, OTP systems are faced with different challenges, among which we can mention the following:

- Attack resiliency [91, 92]
- Key updating [93]

The above discussions suggest the ecosystem of Fig. 1.4 for OTP cryptography.

In Fig. 1.4, *technology* represents *health and medical technology, communication systems, coding systems, financial technology, cloud computing, Internet of Things, and aerospace technology*.

## 1.5.2 The Role of OTP in the Future of Cryptography

As suggested by recent literature, OTP holds a promise for the following modern cryptography paradigms:

- Chaotic cryptography  
In recent years, research on one-time pad cryptography is converging with chaotic cryptography, holding a great promise for both [94, 95].
- A promise for quantum cryptography  
Recent research works suggest that OTP is a good choice for application in quantum cryptography [96, 97].
- A promise for homomorphic encryption  
Homomorphic encryption is another future branch of cryptography that can take advantage of OTP cryptography [98].

Figure 1.5 shows the role of OTP in the future of cryptography.

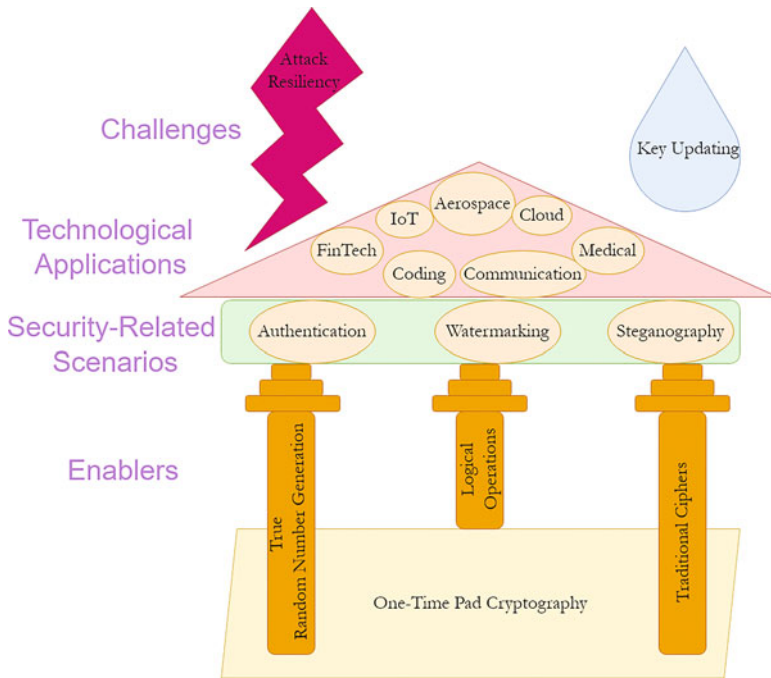


Fig. 1.4 The ecosystem of OTP cryptography

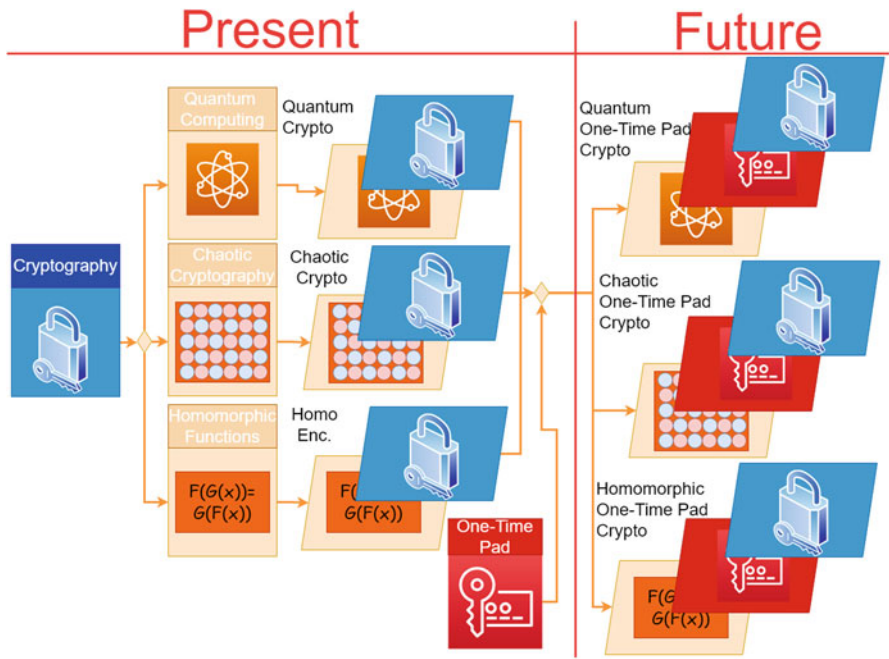


Fig. 1.5 The role of one-time pad in the future of cryptography



# Chapter 2

## Information-Theoretic Cryptography: A Maneuver in the Trade-Off Space of Cryptography in IoT



### 2.1 Introduction and Basic Concepts

IoT systems are resource-constrained environments [99, 99] with real-time requirements [100–102]. On the other hand, there is a big trade-off between real-time and resource-constrained computing [103–105]. This challenging issue shows up in several design aspects of IoT.

The trade-off between timeliness and resource-constrained awareness can be studied in terms of the following trade-offs.

- Performance-area trade-off [106, 107]
- Performance-power trade-off [108, 109]
- Performance-cost trade-off [110, 111]

In this chapter, we focus on the impact of this trade-off on cryptography in IoT. We study the existing trends in research on real-time and resource-constrained cryptography as well as cryptography in IoT in the context of ecosystems and life cycles. Then, we show how these trends converge at information-theoretic cryptography. Our discussions in this chapter suggest information-theoretic cryptography as a promising choice for IoT environments.

The rest of this chapter is organized as follows. Section 2.2 studies real-time cryptography. In this section, we first establish an ecosystem for real-time cryptography. The ecosystem includes *applications* and *enablers*. Under the topic of enablers, we discuss technological applications, applications on different content types, and applications in security-related scenarios. Enablers are the sciences and technologies that support real-time cryptography. The section continues to develop a life cycle for real-time cryptography and study the existing challenges and issues in each phase of the cycle. The life cycle consists of three phases, namely, *design*, *implementation*, and *evaluation*. In the *design* phase, we highlight the objectives considered by researchers while designing real-time cryptosystem. We show that a real-time cryptosystem should be flexible to different design patterns.

Moreover, we demonstrate that real-time cryptosystems need to be compatible with the existing cryptosystems and hold a promise for modern cryptography paradigms. In the *implementation* phase, different challenges are studied; the choice of the base cryptosystem, the choice between hardware and software implementations, and the choice among hardware implementation technologies. In *evaluation* phase, we study evaluation routines, including analysis, cryptanalysis, and attack. Sections 2.3 and 2.4 repeat the above analyses for resource-constrained (embedded and lightweight) cryptography and cryptography in IoT, respectively. Section 2.5 discusses the convergence among real-time cryptography, resource-constrained cryptography, and cryptography in IoT. To this end, this section shows that a common ecosystem and a common life cycle can be imagined for all the three areas and common challenges are faced by researchers in all of the mentioned areas. Lastly, Sect. 2.5.1 shows that information-theoretic cryptography appears almost everywhere in the common ecosystem and the common life cycle. This highlights information-theoretic cryptography as a promising solution for the trade-off between timeliness and resource constraint awareness in IoT cryptography.

## 2.2 Real-Time Cryptography

In the following, we first study the sciences, technologies, and fields of research related to real-time cryptography. These areas form the ecosystem of real-time cryptography when they come together. They are categorized into applications and enablers. Next, we examine the research challenges and issues related to real-time cryptography. We categorize these issues based on the related phases in the life cycle, including design, implementation, and evaluation. These analyses, along with similar analyses on resource-constrained cryptography and cryptography in IoT, suggest a common ecosystem and a life cycle for all of the above fields. Further discussions presented later in this chapter show how the ecosystem and the life cycle of information-theoretic cryptography match the common ecosystem and the common life cycle. This will highlight information-theoretic cryptography as a promising solution for cryptography in IoT.

### 2.2.1 Ecosystem

- Applications  
Real-time cryptography has found its applications in many technological environments. It has been successfully applied on several content types. Moreover, it has been tested in several security-related scenarios. These applications are mentioned in the following.
  - Technological Applications

Real-time cryptography serves to a variety of technological applications. This implies that every approach proposed for real-time cryptography needs the capability of being used in these technological areas. As examples of these areas, one may refer to the following.

- \* Aerospace Technology [112]
  - \* Medical Technology [113, 114]
  - \* Traffic Management Systems [115]
  - \* Multimedia Technology [116]
  - \* Digital Camera [117]
- Applications in Security-Related Scenarios
- The following security-related scenarios frequently appear in the ecosystem of real-time cryptography. This has an implication for every approach proposed for this purpose; it should be applicable in these scenarios.
- \* Privacy [118]
  - \* Authentication [119]
  - \* Forensics [120]
- Application on Different Content Types
- Every approach toward real-time cryptography needs the capacity applied on different content types including the following.
- \* Text [121]
  - \* Image [122, 123]
  - \* Video [124–126]
  - \* Voice [127]
- Enablers
- Different approaches have been taken toward the design of real-time cryptosystems. These approaches highlight different enablers including the ones mentioned below. This makes it necessary for an approach (like the information-theoretic approach) toward real-time cryptography to be capable of taking advantage of these enablers.
- Chaos Theory [123, 124]
  - Hardware Technology [128]
  - Provable Security [129]
  - Artificial Intelligence [130–132]
  - Optical Technology [133]
  - Mathematical Transforms [134]

### 2.2.1.1 Life Cycle

- Design

- Different Design Objectives Considered

In addition to timeliness, as the primary requirement in the design of real-time cryptographic systems, several other objectives have been considered by the research community. Thus, every approach toward real-time cryptography needs the capability of providing a wide range of design objectives.

Among design objectives of real-time cryptography, we may mention the following.

- \* Performance [135] [136]
- \* Security [121, 137]
- \* Fault Tolerance [138]
- \* Integrity [139]
- \* Efficiency [140]
- \* Scalability [115]
- \* Dynamicity [141]
- \* Quality of Experience (QoE) [131, 132]

- Flexible to Different Design Patterns

Different pairwise-opposite cryptographic design patterns can be used for real-time cryptographic purposes. This implies that every approach toward real-time cryptography needs to be compatible with a range of design patterns. Some design patterns used in real-time cryptography are mentioned below.

- \* Block ciphers [142, 143]
- \* Stream ciphers [141, 144, 145]
- \* Symmetric cryptography [146]
- \* Public key cryptography [147, 148]

- Compatible To Existing Cryptosystems

Many existing cryptosystems, including the following ones, can be used as part of solutions for real-time cryptography. This can be considered as an implication for approaches to be proposed in the future.

- \* Elliptic curve cryptosystem (ECC) [135, 149]
- \* Advanced encryption standard (AES) [150]

- A Promising Choice for Modern Cryptographic Paradigms

- \* Homomorphic encryption (HE) [112, 151]
- \* Quantum cryptography [152]

- Implementation

According to recent research works, the following choices can be considered as significant challenges in the implementation phase of real-time cryptosystems.

- Base Cryptosystem [153, 154]

As mentioned earlier in this section, several existing cryptosystems can be used as part of real-time cryptography solutions. Choosing among these cryptosystems is a challenging issue in the implementation phase.

- Hardware/Software Implementation [155]

Once the base cryptosystem is decided, another challenging issue is raised. Real-time cryptosystems can be implemented in hardware or software. Many aspects should be considered to choose between these possible implementations.

- Implementation Technology [156, 157]

Once hardware implementation is chosen, several implementation technologies, such as FPGA, CMOS, etc., can be used for this purpose. Thus, selecting the implementation technology is the next issue.

Every approach must be capable of resolving the above implementation challenges in order to be proper for real-time cryptography.

- Evaluation

Different routines have been considered by researchers in the implementation phase of real-time systems. Among them, we can mention the following.

- Cryptanalysis [158]

- Attack [159, 160]

A newly-proposed approach toward real-time cryptography should pass the above routines and similar ones to find its way into the life cycle of real-time cryptography.

## 2.3 Resource-Constrained Cryptography

In the following, we take a quick look at different aspects of resource-constrained cryptography similar to the case of real-time cryptography. We discuss resource-constrained cryptography in the two following categories.

### 2.3.1 *Embedded Cryptography*

Embedded cryptography is a significant trend in research on resource-constrained cryptography [161–163]. It has received a research focus, especially in recent decades [164, 165]. This topic has been of interest to the academia [166–169].

In the following, we discuss different issues regarding to embedded cryptography, categorized by their related life cycle phases as well as their connection with the ecosystem.

### 2.3.1.1 Ecosystem

- Applications

- Technological Applications
  - \* Video surveillance [115]
  - \* Multimedia technology [170, 171]
  - \* Smart grids [172]
- Applications in Security-Related Scenarios
  - \* Law and forensics [173]
  - \* Visual cryptography [174, 175]
  - \* Information hiding [176, 177]
  - \* Authentication [178, 179]
- Application on Different Content Types
  - \* Image [175, 180, 181]
  - \* Video [171]

- Enablers

Researchers have taken many approaches toward the design of cryptographic primitives to be used in embedded systems. These approaches introduce a range of enablers, among which we can mention the following.

- Hardware technology [167, 182]
- Chaos theory [180, 183]
- Artificial intelligence (AI) [184, 185]
- Compressive sensing [186]

### 2.3.1.2 Life Cycle

- Design

- Different Design Objectives Considered

Resource constraint awareness is obviously the most important design objective in this field. However, researchers have considered several other objectives, including but not limited to the following.

- \* Power consumption [187, 188]
- \* Performance [168, 189]
- \* Scalability [190]
- \* Efficiency (Area efficiency [191])

Efficiency generally refers to the following design objectives.

- Area efficiency [190, 190]
- Cost efficiency [192, 193]

- \* Integrity [194]
- \* Dynamicity [195]
- Flexible to Different Design Patterns
  - \* Stream ciphers [196]
  - \* Block ciphers [197]
  - \* Symmetric cryptography [198, 199]
  - \* Public key cryptography [192, 200]
- Compatible To Existing Cryptosystems
  - \* Elliptic curve cryptography [182, 190]
  - \* AES [191, 201]
  - \* RSA (Rivest-Shamir-Adleman) cryptosystem [202]
  - \* El-Gamal cryptosystem [203]
  - \* McEliece cryptosystem [204]
- A Promising Choice for Modern Cryptographic Paradigms
  - \* Homomorphic encryption [205]
  - \* Pairing-based cryptography [206]
  - \* Quantum cryptography [115, 207]
- Implementation
  - Base cryptosystem [208]
  - Hardware/software implementation [181]
  - Implementation technology [209, 210]
- Evaluation
  - Analysis and formalization [168, 211]
  - Cryptanalysis [169]
  - Attack [212, 213]

### 2.3.2 *Lightweight Cryptography*

Lightweight cryptography is another branch of resource-constrained cryptography. It has rendered a significant trend in this area [214, 215].

In the following, we take a quick look at the ecosystem as well as the life cycle of lightweight cryptography.

#### 2.3.2.1 **Ecosystem**

- Applications
  - Technological Applications

- \* RFID systems [216, 217]
- \* Smart grids [218]
- \* Cloud computing [219, 220]
- \* Fog computing [221]
- \* Sensor networks [222, 223]
- \* Law forensics [224]
- \* Video surveillance [225]
- \* Communication systems [226]
- \* Medical technology [227]
- \* Mobile devices [228]
- \* Vehicular technology [221]
- \* Industrial Internet of Things (IIoT) [229]
- Applications in Security-Related Scenarios
  - \* Authentication [228, 230]
  - \* Secret sharing [231]
  - \* Information hiding [231]
  - \* Privacy [225] [229]
- Application on Different Content Types
  - \* Image [224, 227, 231, 232]
  - \* Video [233, 234]
- Enablers
  - Hardware technology [235]
  - Provable security [236]
  - Chaos theory [237–239]
  - Lattice theory [240]

### 2.3.2.2 Life Cycle

- Design
  - Different Design Objectives Considered

It is obvious that resource constraint awareness is the most critical design objective in this realm. However, several other objectives need to be followed here. To mention a few, we can refer to the following ones.

    - \* Performance [241, 242]
    - \* Power consumption [243]
    - \* Efficiency [244, 245]
    - \* Robustness [224]
    - \* Cost [234]
    - \* Fault tolerance [246]



- \* Scalability [247]
- Flexible to Different Design Patterns
  - \* Symmetric [248–250]
  - \* Public key [228, 251]
  - \* Stream cipher [230, 237]
  - \* Block cipher [248] [252]
- Compatible To Existing Cryptosystems
  - \* Elliptic curve cryptography (ECC) [236, 253]
  - \* AES [254]
  - \* Salsa20 [255]
  - \* PRESENT [241]
- A Promising Choice for Modern Cryptographic Paradigms
  - \* Identity-based encryption (IBE) [256]
  - \* Homomorphic encryption [222] [229, 257]
  - \* White box cryptography [223]
- Implementation
  - Base cryptosystem [258]
  - Hardware/software implementation [240, 252, 259]
  - Implementation technology [246, 260]
- Evaluation
  - Analysis [248, 261, 262]
  - Cryptanalysis [218]
  - Attack [230, 263]

## 2.4 Cryptography in IoT

Different requirements and aspects of cryptography in IoT environments have been of interest to the research community in recent years [264, 265]. In the following, we overview the related ecosystem and the life cycle.

### 2.4.1 *Ecosystem*

- Applications
  - Technological Applications

- \* Cloud computing [266, 267]
- \* Sensor networks [148]
- \* Multimedia technology [268, 269]
- \* Medical technology [270, 271]
- \* Video surveillance [272]
- \* RFID technology [273]
- Applications in Security-Related Scenarios
  - \* Authentication [148, 274]
  - \* Trust [275]
  - \* Privacy [276]
  - \* Information hiding [277, 278]
- Application on Different Content Types
  - \* Image [279, 280]
  - \* Video [268]
- Enablers
  - Hardware technology [281]
  - Chaos theory [282, 283]
  - Lattice theory [267, 284]

### 2.4.1.1 Life Cycle

- Design
  - Different Design Objectives Considered
    - \* Performance [285]
    - \* Cost [283]
    - \* Security [272]
    - \* Efficiency [280]
  - Flexible to Different Design Patterns
    - \* Symmetric cryptography [148, 286]
    - \* Public key cryptography [284, 287, 288]
    - \* Block ciphers [289]
    - \* Stream ciphers [290]
  - Compatible To Existing Cryptosystems
    - \* Elliptic curve cryptography [291]
    - \* AES [292]
    - \* RSA [280]

- A Promising Choice for Modern Cryptographic Paradigms
  - \* Quantum cryptography [282, 293]
  - \* White box cryptography [294]
  - \* Identity-based encryption (IBE) [295]
  - \* Attribute-based encryption (ABE) [296]
  - \* Homomorphic encryption [297]
- Implementation
  - Base cryptosystem [298]
  - Hardware/software implementation [279, 299]
  - Implementation technology [300]
- Evaluation
  - Analysis [297, 301]
  - Cryptanalysis [302]

### 2.4.2 Real-Time Cryptography in IoT

Real-time cryptography in IoT has been of interest to the research community in recent years [303].

Some researchers have added resource constraint awareness to real-time IoT cryptography, which leads to the design of embedded [291] and lightweight [304] IoT cryptography systems. In the following, we establish an ecosystem as well as a life cycle for real-time cryptography in IoT.

#### 2.4.2.1 Ecosystem

- Applications
  - Technological Applications
    - \* Video surveillance [305]
    - \* Medical technology [306]
    - \* Multimedia [305]
    - \* Smart home [307]
  - Applications in Security-Related Scenarios
    - \* Authentication [308]
    - \* Privacy [309]
  - Application on Different Content Types

- \* Image [310]
- \* Video [311]

- Enablers

- Chaos theory [305, 307]
- Fuzzy logic [312]
- Hardware technology [313]
- DNA computing [308]

### 2.4.2.2 Life Cycle

- Design

- Different Design Objectives Considered
  - \* Security [305, 313]
  - \* Performance [314]
- Flexible to Different Design Patterns
  - \* Stream ciphers [315]
  - \* Block ciphers [316]
  - \* Symmetric cryptography [273]
  - \* Public key cryptography [317]
- Compatible To Existing Cryptosystems
  - \* Elliptic curve cryptography (ECC) [291]
  - \* Advanced encryption standard (AES) [307]
- A Promising Choice for Modern Cryptographic Paradigms
  - \* Quantum cryptography [318]
  - \* Homomorphic encryption [151]

- Implementation

- Base Cryptosystem [319]
- Hardware/Software Implementation [313]
- Implementation Technology [314]

- Evaluation

- Attack [320]
- Cryptanalysis [321]

### 2.4.3 *Embedded Cryptography in IoT*

Recent literature comes with several works focusing on embedded cryptography in IoT devices and environments [322]. Different approaches have been taken toward this purpose [186]. The ecosystem and the life cycle of embedded cryptography in IoT are studied below.

#### 2.4.3.1 Ecosystem

- Applications
  - Technological Applications
    - \* Industrial Internet of Things (IIoT) [322]
    - \* Mobile Adhoc NETWORKs (MANETs) [323]
  - Applications in Security-Related Scenarios
    - \* Authentication [324]
    - \* Trust [323]
  - Application on different content types
    - \* Image [272]
    - \* Video [268]
- Enablers
  - Compressive sensing [186]
  - Chaos theory [281]
  - DNA computing [308]

#### 2.4.3.2 Life Cycle

- Design
  - Different Design Objectives Considered
    - \* Performance [325]
    - \* Power [326]
    - \* Efficiency [327]
  - Flexible to Different Design Patterns
    - \* Stream ciphers [315]
    - \* Block ciphers [316]
    - \* Symmetric cryptography [328]

- \* Public key cryptography [329]
- Compatible To Existing Cryptosystems
  - \* Elliptic curve cryptography (ECC) [291]
  - \* ChaCha [315]
- A Promising Choice for Modern Cryptographic Paradigms
  - \* White box Cryptography [330]
  - \* Homomorphic encryption (HE) [303]
  - \* Attribute-base encryption [323, 325]
- Implementation
  - Base Cryptosystem [326]
  - Implementation Technology [325]
  - Hardware/Software Implementation [281, 331]
- Evaluation
  - Analysis [332]
  - Cryptanalysis [321]

## 2.4.4 *Lightweight Cryptography in IoT*

Lightweight cryptography is a recent trend in IoT cryptography [333, 334]. It is of critical application, especially in resource-constrained applications: [335]. The research literature suggests the ecosystem and the life cycle mentioned below for lightweight cryptography in IoT.

### 2.4.4.1 **Ecosystem**

- Applications
  - Technological Applications
    - \* Medical technology [336]
    - \* Cloud computing [337]
  - Applications in Security-Related Scenarios
    - \* Privacy [338]
    - \* Authentication [337]
  - Application on Different Content Types
    - \* Image [339]
    - \* Video [304]

- Enablers
  - Chaos Theory [340]
  - DNA Technology [341]
  - Hardware Technology [342, 343]

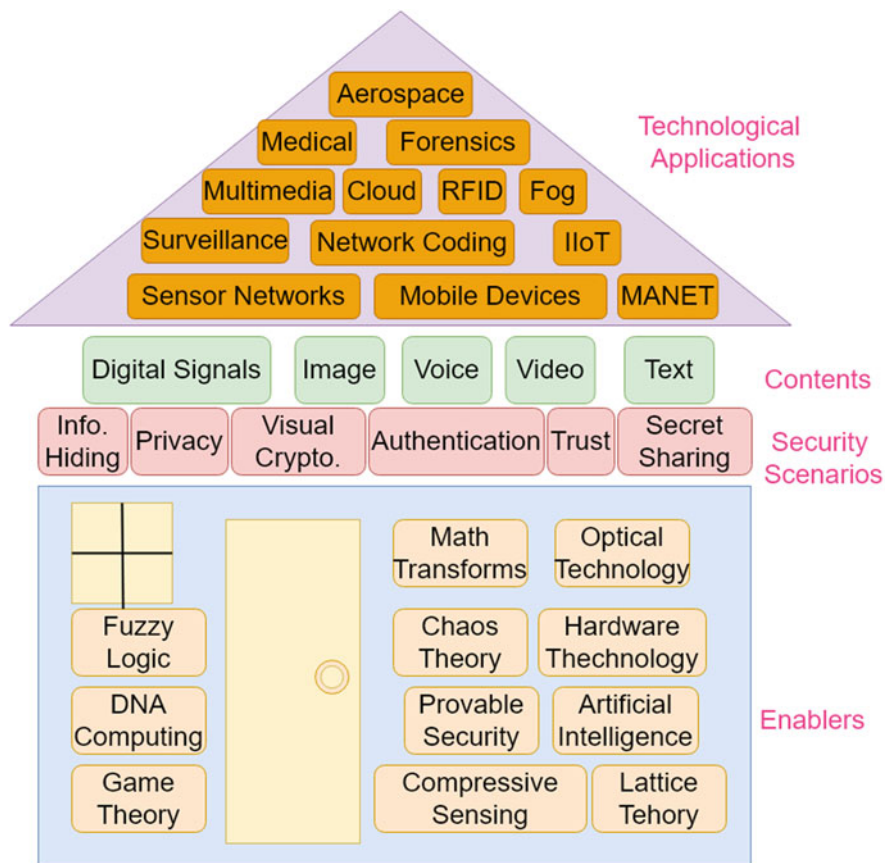
#### 2.4.4.2 Life Cycle

- Design
  - Different Design Objectives Considered
    - \* Performance [338, 344, 345]
    - \* Power [346, 347]
    - \* Security [339, 348]
    - \* Efficiency [349]
    - \* Robustness [337]
  - Flexible to Different Design Patterns
    - \* Stream ciphers [350]
    - \* Block ciphers [351–353]
    - \* Symmetric cryptography [339, 354]
    - \* Public key cryptography [342, 355]
  - Compatible To Existing Cryptosystems
    - \* Blowfish [339]
    - \* Elliptic curve cryptography (ECC) [343]
  - A Promising Choice for Modern Cryptographic Paradigms
    - \* White box cryptography [356]
    - \* Identity-based encryption [357]
- Implementation
  - Base Cryptosystem [339, 348]
  - Implementation Technology [343]
- Evaluation
  - Analysis [338, 345]
  - Attack [320, 348]
  - Cryptanalysis [358]

## 2.5 Convergence: Matching Ecosystems, Life Cycles, and Challenges

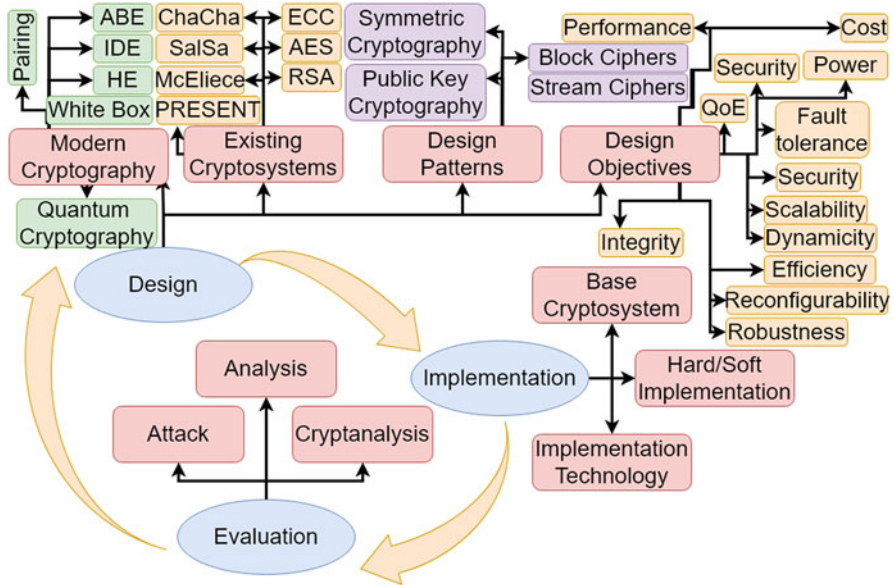
According to the above discussions, the ecosystem of Fig. 2.1 is more or less applicable to the following areas.

- Real-time cryptography
- Resource-constrained cryptography
- Cryptography in IoT
- Real-time cryptography in IoT
- Resource-constrained cryptography in IoT



**Fig. 2.1** The ecosystem (as suggested by research literature) for real-time cryptography, resource-constrained cryptography, cryptography in IoT, real-time cryptography in IoT, and resource-constrained cryptography in IoT





**Fig. 2.2** The life cycle and related issues (as suggested by research literature) for real-time cryptography, resource-constrained cryptography, cryptography in IoT, real-time cryptography in IoT, and resource-constrained cryptography in IoT

Similarly, the life cycle of Fig. 2.2, as well as the related issues shown in this figure, is more or less applicable to the areas mentioned above.

- Real-time cryptography
- Resource-constrained cryptography
- Cryptography in IoT
- Real-time cryptography in IoT
- Resource-constrained cryptography in IoT

### ***2.5.1 Information-Theoretic Cryptography: The Convergence Point***

In the following, we discuss the role of information theory in IoT cryptography as well as real-time and resource-constrained cryptography. These discussions suggest information theory as a proper approach toward real-time and resource-constrained cryptography in IoT.

### 2.5.1.1 Ecosystem

- Applications
  - Technological Applications
    - \* Network coding [359]
    - \* Cloud computing [360]
    - \* Mobile Adhoc NETWORKS (MANETs) [361]
    - \* Power systems [362]
  - Applications in Security-Related Scenarios
    - \* Privacy [363]
    - \* Information hiding [364, 365]URRU-Jour006
  - Application on Different Content Types
    - \* Digital signals [366]
    - \* Video [367, 368]
    - \* Image [369–371]
- Enablers
  - Provable security [372, 373]
  - Mathematical transforms [374]
  - Game theory [17, 375]
  - Chaos theory [371, 376]
  - Compressive sensing [377]

### 2.5.1.2 Life Cycle

- Design
  - Different Design Objectives Considered
    - \* Performance [378]
    - \* Efficiency [379]
    - \* Fault tolerance [380]
    - \* Dynamicity [381]
  - Flexible to Different Design Patterns
    - \* Stream ciphers [363, 373, 382]
    - \* Block ciphers [380, 383]
    - \* Symmetric cryptography [384]
    - \* Public key cryptography [385]
  - Compatible To Existing Cryptosystems

- \* RSA [382]
- \* RC6 [382]
- \* Elliptic curve cryptography [379]
- A Promising Choice for Modern Cryptographic Paradigms
  - \* Quantum cryptography [386]
  - \* Homomorphic encryption [387]
  - \* White box cryptography [388]
- Implementation
  - Base cryptosystem [380]
- Evaluation
  - Analysis and formalization [15, 389, 390]
  - Cryptanalysis [16, 391, 392]

The matching ecosystems and life cycles have made it possible for information-theoretic cryptography to be successfully tested in the following areas.

### ***2.5.2 Information-Theoretic Cryptography in IoT***

Perfect secrecy [393, 394] and especially OTP [89] have been widely used for cryptography in IoT. Information theory has been specially used in the design of cryptographic devices, such as physically unclonable functions (PUFs) [395, 395, 396] to be used in IoT. In addition to encryption, information theory has been used to conduct attacks against IoT cryptography systems [397].

### ***2.5.3 Information-Theoretic Cryptography in Real-Time and Resource-Constrained Applications***

Many researchers have focused on the applications of information-theoretic cryptography in real-time [139], embedded [398], and lightweight [361] applications.

#### **Lightweight**

Multimedia [388]

### ***2.5.4 Information-Theoretic Cryptography in Real-Time and Resource-Constrained IoT***

As expected, information-theoretic cryptography is of great application in real-time computing environments [139, 139].

Moreover, recent literature highlights information-theoretic cryptography as a promising solution for embedded [398] and lightweight [72, 72, 399, 400] applications.

## Part II

# Combinatorial-Boolean Approach Toward Perfect Secrecy in IoT

In Part I, we studied information-theoretic cryptography and showed how it can resolve the trade-off between real-time and resource-constraint requirements of cryptography in IoT. Part I justifies our choice of information-theoretic cryptography to fulfill the requirements of IoT.

In this part, we first take one step forward and state our reasons for choosing a hybrid combinatorial-Boolean approach toward information-theoretic cryptography. Then, we formalize our proposed approach.

This part consists of three chapters. The first chapter studies combinatorial cryptography with a focus on Latin squares and their applications in cryptography. In this chapter, we first take a look at the role of combinatorics in cryptography. We continue to introduce some squares with applications in cryptography. Next, we investigate combinatorial squares and cubes including Latin/magic squares and cubes and show how they are used in cryptography and related areas. We especially study Latin squares along with technological applications as well as related theories and applications in cryptography, variants, generalizations and extensions, related problems, and challenges.

The second chapter is about Boolean cryptography. In this chapter, we first explain how the cryptography research community is taking advantage of Boolean algebra, Boolean functions and mappings, Boolean maskings, Boolean problems, Boolean permutations and substitutions, and Boolean queries over encrypted data. Then, we take a look at the position of Boolean cryptography in the ecosystem as well as the life cycle of information-theoretic cryptography.

The third chapter introduces our proposed approach. In this chapter, we first present a Boolean method based on *Resilient* Boolean functions for formal description as well as encoding of encryption and decryption algorithms. Next, we use the method to formalize and encode perfectly secure cryptographic algorithms. This paves the way for presenting a conceptual model for *random key random algorithm* perfectly secure cryptography. In the next step, we connect our method with Latin squares. Lastly, we reason why our method can be efficiently used in IoT environments.

# Chapter 3

## Combinatorial Cryptography and Latin Squares



### 3.1 Introduction

Combinatorics refers to a branch of mathematics that discusses methods for enumerating the number of possible ways for doing something. It has applications in statistics, probabilities, and many other scientific fields. This section focuses on the applications of combinatorics in cryptography. There are some combinatorial puzzles that appear in the form of squares and cubes. Counting the number of ways to fill each these puzzles is a combinatorial problem. We specially focus on cryptographic applications of these puzzles. Among these puzzles, Latin squares will be used in our approach toward information-theoretic cryptography, which is introduced in the last chapter of this book.

The rest of this chapter is organized as follows. Section 3.2 presents an overview on the cryptographic applications of combinatorics. Section 3.3 studies some historical ciphers that use non-combinatorial squares as part of their structures. In this section, we study different cryptographic squares such as Polybius square, Playfair square, and Vigenere square. Moreover, we examine some square-based ciphers including two-square and four-square ciphers. Section 3.4 investigates cryptographic combinatorial squares and cubes. In this section, we first study some square combinatorial designs, such as Howell design, Room square, and Hadamard matrices. Then, we focus on combinatorial square and cube designs along with their cryptographic applications. Among these designs, Latin squares are of more importance, as they are used in the approach proposed in this book toward information-theoretic cryptography in IoT. In Sect. 3.4, we specifically examine the cryptographic properties of Latin squares as well as their applications in cryptographic mechanisms. Furthermore, we highlight the random generation of Latin squares as a highly challenging issue in this area. We will get back to this problem later in this book while explaining our proposed method for information-theoretic cryptography in IoT.

## 3.2 Combinatorics and Cryptography

The application of combinatorics in cryptography dates back to past decades [401–403]. Moreover, this branch of cryptography is still of interest to researchers [404, 405].

The applications of combinatorics in cryptography can be explained in the following categories.

- Applications of combinatorial optimization in cryptography [406]
- Applications of combinatorial group theory in cryptography [407, 408]
- Applications of combinatorial constructs in cryptography [409]
- Applications of combinatorial designs in cryptography [410–412]
- Applications of combinatorial puzzles in cryptography [413]

In this section, we will focus on combinatorial puzzles and especially on square and cube combinatorial puzzles, along with their cryptographic applications. To begin our discussions in this area, let us first take a look at the history.

## 3.3 A Look at the History: Cryptographic Squares and Square-Based Cryptography

Similar to the case of combinatorics, squares have been historically used in cryptography. Among (non-combinatorial) squares used in cryptography, one may refer to the following.

- Polybius Square: Recent Years [414]

The Polybius square plays the role of a substitution box that maps each alphabet letter to a two-digit number. For each letter, the leftmost digit is the related row number, and the rightmost one is the column number, both extracted from Fig. 3.1.

**Fig. 3.1** The Polybius square

	1	2	3	4	5
1	A	B	C	D	E
2	F	G	H	I/J	K
3	L	M	N	O	P
4	Q	R	S	T	U
5	V	W	X	Y	Z

Put more formally, suppose the total order  $\Omega$  defined as  $A < B < C < \dots < X < Y < Z$ . Let function  $\mathcal{M}$ , defined with following rules, map each element  $\omega \in \Omega$  to  $\mathcal{M}(\omega)$ .

$$\begin{cases} \forall \omega \in \Omega : \mathcal{M} \in [1, 26] \\ \forall \omega_1, \omega_2 \in \Omega : \omega_1 < \omega_2 \Rightarrow \mathcal{M}(\omega_1) < \mathcal{M}(\omega_2) \end{cases}$$

Now let us define functions  $(D)_1$  and  $(D)_2$  as follows.

$$(D)_1(\omega) = \begin{cases} (\mathcal{M}(\omega) \div 5) + 1 & \mathcal{M}(\omega) \leq 10 \\ ((\mathcal{M}(\omega) - 1) \div 5) + 1 & \mathcal{M}(\omega) > 10 \end{cases}$$

$$(D)_2(\omega) = \begin{cases} \mathcal{M}(\omega) \bmod 5 & \mathcal{M}(\omega) \leq 10 \\ (\mathcal{M}(\omega) - 1) \bmod 5 & \mathcal{M}(\omega) > 10 \end{cases}$$

The Polybius square converts each  $\omega \in \Omega$  to  $10(D)_2(\omega) + (D)_1(\omega)$ .

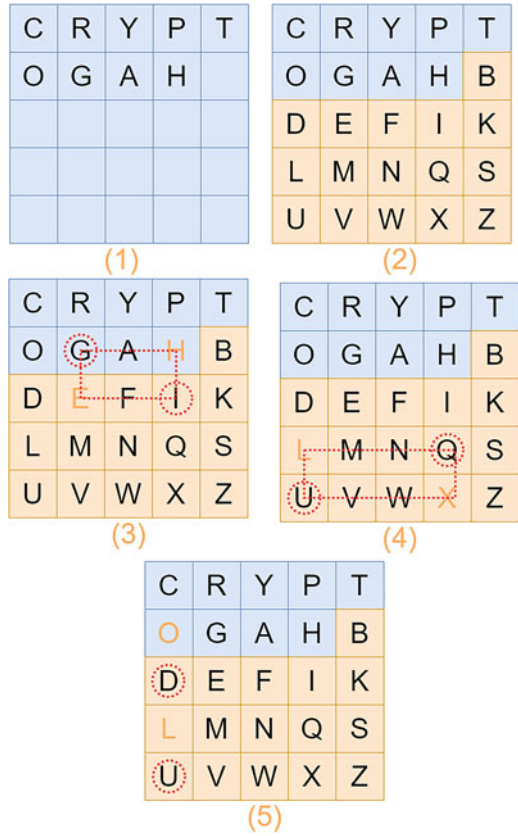
- Playfair Square: Recent Years [415]

The Playfair square is a  $5 \times 5$  square that contains all the alphabet letters except for *J*. Playfair cipher uses an agreed-upon key in the form of a character string. The cells of the square are filled from left to right and from top to down. The first cells are filled with the key such that each character occurs once. For example, if *CRYPTOGRAPHY* is the key, the cells are filled with *C, R, Y, P, T, O, G, A,* and *H* (please see the square number (1) in Fig. 3.2). Then, the rest of the remaining cells are filled with the remaining characters (shown by the square number (2) in Fig. 3.2). Now the square is ready for encryption according to the following rules.

1. Any occurrence of *J* should be dropped from the plain text.
2. Pairs of repeated letters are broken via inserting and *X*. For example, *LL* is converted to *LXL*.
3. The remaining plain text is broken into pairs of letters.
4. A single letter at the end of the string is paired with an extra *Z*.
5. Each pair of letters is substituted by another pair of letters after being located in the Playfair square according to the rules below.
  - (a) If both letters are in the same column, each one is substituted by the letter below it (going back to the top if necessary).
  - (b) If both letters are in the same row, each one is substituted by its right side letter (going back to the left if necessary).
  - (c) Otherwise, the two letters highlight two opposite corners of a rectangle. In this case, the two characters in the remaining corners of the same rectangle are substituted.



**Fig. 3.2** The Playfair cipher encrypting “HELLO” to “GIQUDU”



Squares (3), (4), and (5) show how this cipher encrypts *HELLO* to *GIQUDU*.

- Two-Square and Four-Square Ciphers [416]  
The two-square cipher uses two Playfair squares with two different key strings. The encryption rules are similar to those of Playfair cipher except that each pair of letters is searched in both squares (please see [417] for more information). The four-square cipher is a further extended version of the Playfair cipher [418].
- Vigenere Square [419]

Figure 3.3 shows the Vigenere square.

The Vigenere cipher works as follows. First, the key is repeated until its length reaches that of the plain text. For example, If the plain text is *ATTACKATDAWN*, the key *HELLO* should be extended to *HELLOHELLOHE*. Then, each letter in the cipher text is substituted by the letter in the Vigenere square, whose row is designated by the plain text character and the column is specified by the corresponding key letter. For example, the *C* in the cipher text is encrypted to *Q*, which lies in row *C* and column *O*.

	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z
A	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z
B	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A
C	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B
D	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C
E	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D
F	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E
G	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F
H	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G
I	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H
J	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I
K	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J
L	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K
M	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L
N	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M
O	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N
P	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O
Q	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P
R	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q
S	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R
T	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S
U	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T
V	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U
W	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V
X	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W
Y	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X
Z	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y

Fig. 3.3 The Vigenere square

In addition to squares, some kinds of cubes have been used in cryptography [420].

### 3.4 Cryptographic Combinatorial Squares and Cubes (Puzzles)

So far, different square and cube combinatorial designs have been of interest to the cryptography research community.

- Howell Design [421]  
 Let  $S$  be a set of  $2n$  symbols; then, a Howell design  $H(s, 2n)$  on  $S$  is an  $s \times s$  square  $H$  such that

1. Every cell in  $H$  is either empty or filled with a 2-subset of  $S$ .
  2. Every symbol of  $S$  occurs exactly once in each row and each column of  $H$ .
  3. Every 2-subset of  $S$  occurs in at most one cell of  $H$ .
- Room Square [422]  
 A Room square (named after T. G. Room) of order  $n = 2k$  is an  $(n - 1) \times (n - 1)$  square built on a set  $S$  of objects ( $|S| = n$ ) with the following criteria.
    1. Each cell is either empty or holds a 2-subset of  $S$ .
    2. Each element  $s \in S$  appears exactly once in each row and each column.
    3. Each 2-subset occupies exactly one cell.

The set of Room squares is obviously a subset of the set of Howell designs. A Room square of order 8 is shown in Fig. 3.4.

- Hadamard Matrices [423–425]  
 A Hadamard matrix  $H_d$  of order  $n$  is an  $n \times n$  square matrix, provided that  $\forall i, j \in [1, n], H_d[i, j] \in \{-1, 1\}$ , and  $H_d \cdot H_d^T = I_n$ .  
 Two Hadamard matrices of orders 4 and 8 can be seen in Fig. 3.5.

In the rest of this chapter, we focus on Latin/magic squares/cubes because of their popularity.

**Fig. 3.4** A Room square of order 8

{1,8}		{5,7}		{3,4}{2,6}
{3,7}{2,8}		{1,6}		{4,5}
{5,6}{1,4}{3,8}			{2,7}	
	{6,7}{2,5}{4,8}			{1,3}
{2,4}	{1,7}{3,6}{5,8}			
	{3,5}	{1,2}{4,7}{6,8}		
		{4,6}	{2,3}{1,5}{7,8}	

**Fig. 3.5** Two Hadamard matrices of orders 4 and 8

1	1	1	1
1	-1	1	-1
1	1	-1	-1
1	-1	-1	1

(4)

1	1	1	1	1	1	1	1
1	-1	1	-1	1	-1	1	-1
1	1	-1	-1	1	1	-1	-1
1	-1	-1	1	1	-1	-1	1
1	1	1	1	-1	-1	-1	-1
1	-1	1	-1	-1	1	-1	1
1	1	-1	-1	-1	-1	1	1
1	-1	-1	1	-1	1	1	-1

(8)

### 3.5 Latin/Magic Squares and Cryptography

In this section, we study Latin and magic squares and study their applications in cryptography.

#### 3.5.1 Latin Square

An  $n \times n$  matrix  $[\mathcal{S}^{(L)}]_{n \times n}$  represents a Latin square of order  $n$  if it satisfies Eq. (3.1):

$$\forall i, j \in \{1, 2, \dots, n\} : \begin{cases} \{x | \exists k \in \{1, 2, \dots, n\} : \mathcal{S}^{(L)}[i, k] = x\} = \{1, 2, \dots, n\}, \\ \{x | \exists k \in \{1, 2, \dots, n\} : \mathcal{S}^{(L)}[k, j] = x\} = \{1, 2, \dots, n\}. \end{cases} \quad (3.1)$$

As an example,  $[\mathcal{S}^{(L)}]_{10 \times 10}$  in Eq. (3.2) is a Latin square of order 10.

$$\mathcal{S}^{(L)} = \begin{bmatrix} 1 & 8 & 9 & 10 & 2 & 4 & 6 & 3 & 5 & 7 \\ 7 & 2 & 8 & 9 & 10 & 3 & 5 & 4 & 6 & 1 \\ 6 & 1 & 3 & 8 & 9 & 10 & 4 & 5 & 7 & 2 \\ 5 & 7 & 2 & 4 & 8 & 9 & 10 & 6 & 1 & 3 \\ 10 & 6 & 1 & 3 & 5 & 8 & 9 & 7 & 2 & 4 \\ 9 & 10 & 7 & 2 & 4 & 6 & 8 & 1 & 3 & 5 \\ 8 & 9 & 10 & 1 & 3 & 5 & 7 & 2 & 4 & 6 \\ 2 & 3 & 4 & 5 & 6 & 7 & 1 & 8 & 9 & 10 \\ 3 & 4 & 5 & 6 & 7 & 1 & 2 & 10 & 8 & 9 \\ 4 & 5 & 6 & 7 & 1 & 2 & 3 & 9 & 10 & 8 \end{bmatrix} \quad (3.2)$$

A Latin square  $[\mathcal{S}^{(L)}]_{n \times n}$  is referred to as a normalized (reduced) Latin square if  $\forall i, j \in \{1, 2, \dots, n\} : (\mathcal{S}^{(L)}[i, 1] = i \wedge \mathcal{S}^{(L)}[1, j] = j)$ . Let  $[\mathcal{S}_1^{(L)}]_{n \times n}$  and  $[\mathcal{S}_2^{(L)}]_{n \times n}$  be two Latin squares.  $\mathcal{S}_1^{(L)}$  and  $\mathcal{S}_2^{(L)}$  are said to be orthogonal if  $|\{(x, y) | \exists i, j \in \{1, 2, \dots, n\} : \mathcal{S}_1^{(L)}[i, j] = x \wedge \mathcal{S}_2^{(L)}[i, j] = y\}| = n^2$ .

In this paper, we represent the set of all Latin squares of order  $n$  by  $\mathcal{U}_{SL|n}$ . There is no easily computable explicit formula for  $|\mathcal{U}_{SL|n}|$ , where  $n$  is an arbitrary positive integer. However, the value of  $|\mathcal{U}_{SL|n}|$  is known for  $n \in \{1, 2, \dots, 11\}$  [426], and it is well-known that  $|\mathcal{U}_{SL|n}| = n!(n-1)!|\mathcal{U}_{SL|n}|$ , where  $\mathcal{U}_{SL|n}^{(N)}$  is the number of normalized Latin square of order  $n$ . Furthermore, there are some lower and upper bounds for  $|\mathcal{U}_{SL|n}|$ , such as the ones given by Inequality 3.3 [427],

$$\frac{(n!)^{2n}}{n^{n^2}} \leq |\mathcal{U}_{SL|n}| \leq \prod_{k=1}^n (k!)^{\frac{n}{k}}. \quad (3.3)$$

To cite [428–436]

**Related Theories with Applications in Cryptography** Some theories supporting Latin squares have been of interest to the cryptography research community. Among these theories, we can mention the following.

- Quasigroups Theory [437, 438]
- Permutation Groups Theory [439, 440]
- Symmetric Groups [441]

### 3.5.1.1 Variants, Generalizations, and Extensions

The literature comes with cryptographic applications for different variants, generalizations, and extensions of Latin squares, some of which are discussed below.

- Sudoku [442, 443]

A Sudoku is a Latin square of order 9 partitioned into a  $3 \times 3$  grid of  $3 \times 3$  regions, such that each  $i \in \{1, 2, \dots, 9\}$  occurs exactly once in each region. For example,  $\mathcal{S}^{(S)}$  in Eq. (3.4) demonstrate a Sudoku.

$$\mathcal{S}^{(S)} = \begin{bmatrix} \begin{bmatrix} 8 & 2 & 7 \\ 9 & 6 & 5 \\ 3 & 4 & 1 \end{bmatrix} & \begin{bmatrix} 1 & 5 & 4 \\ 3 & 2 & 7 \\ 6 & 8 & 9 \end{bmatrix} & \begin{bmatrix} 3 & 9 & 6 \\ 1 & 4 & 8 \\ 7 & 5 & 2 \end{bmatrix} \\ \hline \begin{bmatrix} 5 & 9 & 3 \\ 4 & 7 & 2 \\ 6 & 1 & 8 \end{bmatrix} & \begin{bmatrix} 4 & 6 & 8 \\ 5 & 1 & 3 \\ 9 & 7 & 2 \end{bmatrix} & \begin{bmatrix} 2 & 7 & 1 \\ 6 & 8 & 9 \\ 4 & 3 & 5 \end{bmatrix} \\ \hline \begin{bmatrix} 7 & 8 & 6 \\ 1 & 5 & 4 \\ 2 & 3 & 9 \end{bmatrix} & \begin{bmatrix} 2 & 3 & 5 \\ 7 & 9 & 6 \\ 8 & 4 & 1 \end{bmatrix} & \begin{bmatrix} 9 & 1 & 4 \\ 8 & 2 & 3 \\ 5 & 6 & 7 \end{bmatrix} \end{bmatrix} \quad (3.4)$$

- Frequency Latin Square [444]

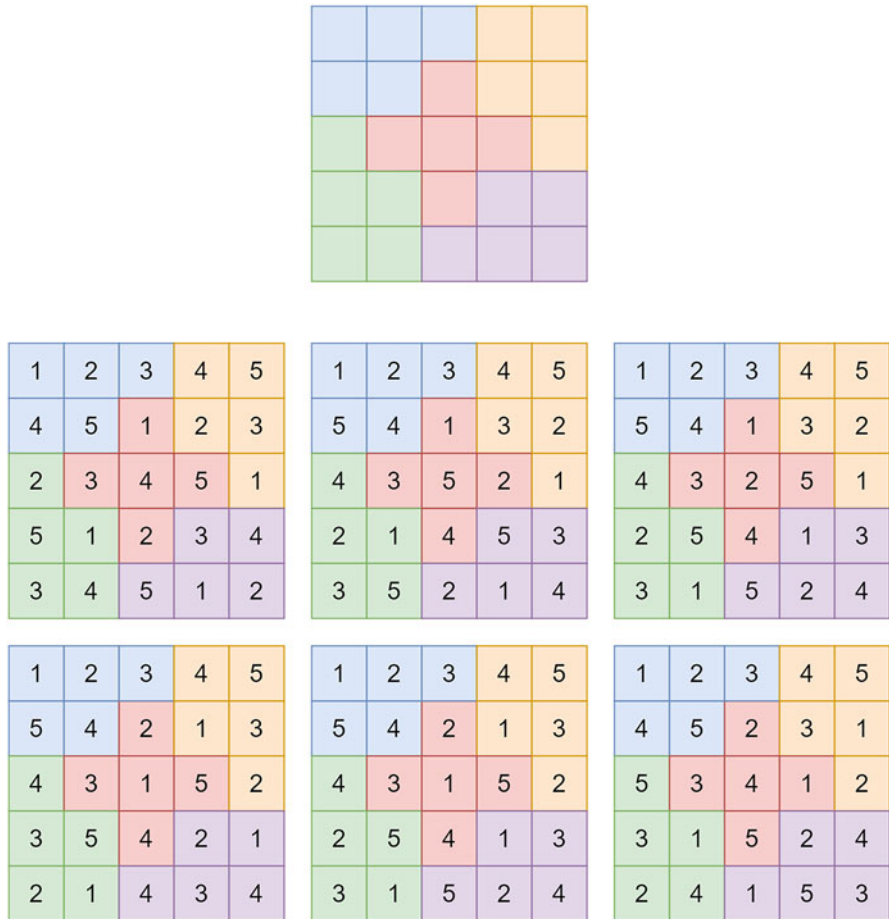
An  $(n, m)$  frequency Latin square is an  $n.m \times n.m$  square, where each  $n$  symbol occurs exactly  $m$  times in each row and each column.

$$\mathcal{S}^{(F_q)} = \begin{bmatrix} 0 & 1 & 0 & 1 \\ 1 & 0 & 1 & 0 \\ 0 & 1 & 0 & 1 \\ 1 & 0 & 1 & 0 \end{bmatrix} \quad (3.5)$$

- Gerechte Design [445]

A gerechte design is an  $n \times n$  grid partitioned into  $n$  regions (Not necessarily in the form of squares), each containing  $n$  cells of the grid, such that each of the symbols 1 through  $n$  occurs exactly once in each row, column, or region.

Figure 3.6 shows a set of gerechte designs of order 5.



**Fig. 3.6** A set of gerechte designs order 5

All the designs in Fig. 3.6 follow a single partitioning scheme. This scheme is seen in the upside of the figure.

- KenKen Puzzle [446, 447]  
 A KenKen puzzle is a Latin square partitioned to a number of cages (regions), not necessarily of identical sizes.  
 There is a predefined number along with a predefined algebraic operation.  
 The numbers in each cage must combine—in any order—to produce the cage’s target number using the indicated math operation. Numbers may be repeated within a cage as long as rule 2 isn’t violated.  
 Figure 3.7 illustrates a sample KenKen puzzle before and after being filled.

**Fig. 3.7** A KenKen puzzle before and after being filled



### 3.5.1.2 Related Problems and Challenges

The research community have posed several problems in regard with Latin squares. Some of these problems are as follows.

- Create[448]
- Enumeration [449]
- Relation with other mathematical constructs [450]

Among the applications of Latin squares, one may refer to the following.

### 3.5.1.3 Applications

The research literature suggests the following applications for Latin squares.

- Applications in Coding
  - Some research works have focused on the applications of Latin squares in the following categories of codes.
  - Liberation codes [451]
  - Error correction codes [452–454]
  - Erasure codes [455]
- Communication systems [456]
- Control systems [457]
- Computer memory systems [458, 459]

## 3.5.2 Magic Square

A magic square of order  $n$  is represented by an  $n \times n$  matrix  $[S^{(M)}]_{n \times n}$  that satisfies Eqs. (3.6), (3.7), (3.8), and (3.8),

$$\{x|\exists i, j \in \{1, 2, \dots, n\} : S^{(M)} [i, j] = x\} = \{1, 2, \dots, n\}, \tag{3.6}$$

$$\forall i, j \in \{1, 2, \dots, n\} : \begin{cases} \sum_{k=1}^n \mathcal{S}^{(M)} [i, k] = \mathcal{M}(n), \\ \sum_{k=1}^n \mathcal{S}^{(M)} [k, j] = \mathcal{M}(n), \end{cases} \quad (3.7)$$

$$\sum_{k=1}^n \mathcal{S}^{(M)} [k, k] = \sum_{k=1}^n \mathcal{S}^{(M)} [k, n+1-k] = \mathcal{M}(n), \quad (3.8)$$

where  $\mathcal{M}(n) = \frac{\sum_{t=1}^{n^2} t}{n} = \frac{n(n^2+1)}{2}$ .

A sample magic square of order 4 is given by Eq. (3.9),

$$\mathcal{S}^{(M)} = \begin{bmatrix} 16 & 3 & 2 & 13 \\ 5 & 10 & 11 & 8 \\ 9 & 6 & 7 & 12 \\ 4 & 15 & 14 & 1 \end{bmatrix}. \quad (3.9)$$

In recent years, researchers have been interested in several applications of magic squares [460] as well as several related problems [461]. In this book,  $\mathcal{U}_{SM|n}$  represents the number of magic squares of order  $n$ . This value is known for  $1 \leq n \leq 5$  [462]. However, the problem of calculating  $|\mathcal{U}_{SM|n}|$  for an arbitrary  $n$  is still unsolved.

### 3.5.2.1 Franklin Squares as Variants of Magic squares

A Franklin square of order  $n$  is a magic square of order  $n$ , wherein the numbers in the bend diameters sum up to  $\frac{n(n^2+1)}{2n}$ , referred to as the magic constant. Moreover, in a Franklin square, the numbers in the four corners and four central cells sum up to the magic constant.

As an example,  $[\mathcal{S}_1^{(F_k)}]_{8 \times 8}$  in Eq. (3.10) and  $[\mathcal{S}_2^{(F_k)}]_{8 \times 8}$  in Eq. (3.11) are Franklin squares of order 8.

$$\mathcal{S}_1^{(F_k)} = \begin{bmatrix} 52 & 61 & 4 & 13 & 20 & 29 & 36 & 45 \\ 14 & 3 & 62 & 51 & 46 & 35 & 30 & 19 \\ 53 & 60 & 5 & 12 & 21 & 28 & 37 & 4 \\ 11 & 66 & 59 & 54 & 43 & 38 & 27 & 22 \\ 55 & 58 & 7 & 10 & 23 & 26 & 39 & 42 \\ 9 & 8 & 57 & 56 & 41 & 40 & 25 & 24 \\ 50 & 63 & 2 & 15 & 18 & 31 & 34 & 47 \\ 16 & 1 & 64 & 49 & 48 & 33 & 32 & 17 \end{bmatrix} \quad (3.10)$$



200	217	232	249	8	25	40	57	72	89	104	121	136	153	168	1185
58	39	26	7	250	231	218	199	186	167	154	135	122	103	90	71
198	219	230	251	6	27	38	59	70	91	102	123	134	155	166	187
60	37	28	5	252	229	220	197	188	165	156	133	124	101	92	69
201	216	233	248	9	24	41	56	73	88	105	120	137	152	169	184
55	42	23	10	247	234	215	202	183	170	151	138	119	106	87	74
203	214	235	246	11	22	43	54	75	86	107	118	139	150	171	182
53	44	21	12	245	236	213	204	181	172	149	140	117	108	85	76
205	212	237	244	13	20	45	52	77	84	109	116	141	148	173	180
51	46	19	14	243	238	211	206	179	174	147	142	115	110	83	78
207	210	239	242	15	18	47	50	79	82	111	114	143	146	175	178
49	48	17	16	241	240	209	208	177	176	145	144	113	112	81	80
196	221	228	253	4	29	36	61	68	93	100	125	132	157	164	189
62	35	30	3	254	227	222	195	190	163	158	131	126	99	94	67
194	223	226	255	2	31	34	63	66	95	98	127	130	159	162	191
64	33	32	1	256	225	224	193	192	161	160	129	128	97	96	65

Fig. 3.8 A Franklin square of order 16

$$S_2^{(F_k)} = \begin{bmatrix} 17 & 47 & 30 & 36 & 21 & 43 & 26 & 40 \\ 32 & 34 & 19 & 45 & 28 & 38 & 23 & 41 \\ 33 & 31 & 46 & 20 & 37 & 27 & 42 & 24 \\ 48 & 18 & 35 & 29 & 44 & 22 & 39 & 25 \\ 49 & 15 & 62 & 4 & 53 & 11 & 58 & 8 \\ 64 & 2 & 51 & 13 & 60 & 60 & 55 & 9 \\ 1 & 63 & 14 & 52 & 5 & 59 & 10 & 56 \\ 16 & 50 & 3 & 61 & 12 & 54 & 7 & 57 \end{bmatrix} \tag{3.11}$$

Moreover, a Franklin square of order 16 is seen in Fig. 3.8.

Franklin squares have been of special interest to the cryptography research community [463–465].

### 3.5.2.2 Solving Magic Squares: The Main Related Problem

As suggested by the research literature, solving the magic square puzzle is the most critical problem in this area [466–468].

### 3.5.2.3 Applications

Magic squares have found their many applications in technology, science, and arts. Some of their application areas are as follows.

- Applications in Technology
  1. Communications [469, 470]
  2. Power grid control [471]
  3. Image processing [472]
  4. Digital to analogue converters [473, 474]
  5. Applications in science and art
    - Applications in optimization [475]
    - Applications in aesthetics [476]

## 3.6 Latin/Magic Cubes and Cryptography

In this section, we discuss Latin and magic cubes and study their applications in cryptography.

### 3.6.1 Latin Cube

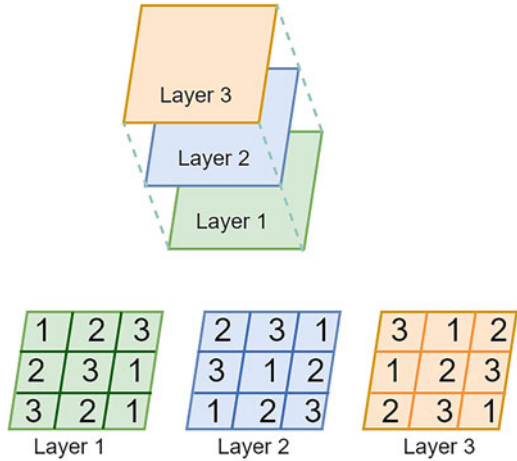
Consider  $n \in \mathbb{N} \setminus \{1\}$ ; an  $n \times n \times n$  matrix  $[C^{(L)}]_{n \times n \times n}$  represents a Latin cube of order  $n$  if it satisfies Eq. (3.12),

$$\forall i, j, k \in \{1, 2, \dots, n\} : \begin{cases} \{x | \exists t \in \{1, 2, \dots, n\} : C^{(L)}[i, j, t] = x\} = \{1, 2, \dots, n\}, \\ \{x | \exists t \in \{1, 2, \dots, n\} : C^{(L)}[i, t, k] = x\} = \{1, 2, \dots, n\}, \\ \{x | \exists t \in \{1, 2, \dots, n\} : C^{(L)}[t, j, k] = x\} = \{1, 2, \dots, n\}. \end{cases} \quad (3.12)$$

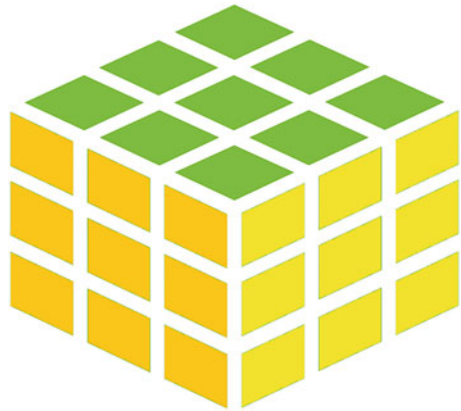
Figure 3.9 shows a sample Latin cube of order 3.

Researchers have studied different types [477] and applications [478, 479] of Latin cubes, along with different related problems [480].

**Fig. 3.9** A Latin cube of order 3



**Fig. 3.10** A Rubik cube



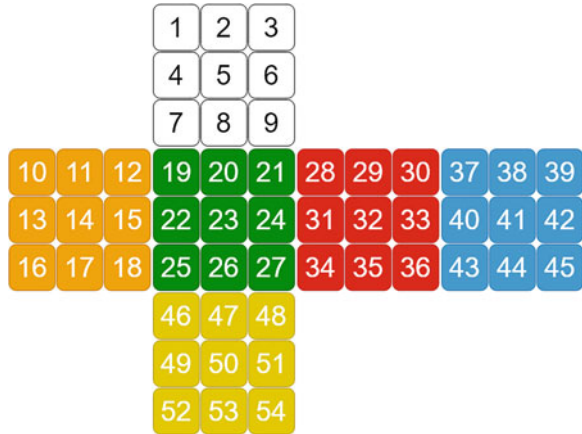
### 3.6.2 Magic Cube

Rubik's cube has been of special interest to cryptography research community in recent years [481, 482]. Magic cube a.k.a Rubik cube was invented by Rubik Erno in 1974. Using a cube with 54 equally sized squares of 6 different colors on its 6 faces, Rubik cube represents an ordered list of 54 instances of 6 different numbers (e.g., 1 through 6), where each number is repeated exactly 9 times. In this cube, colors represent numbers. Figure 3.10 shows a Rubik cube.

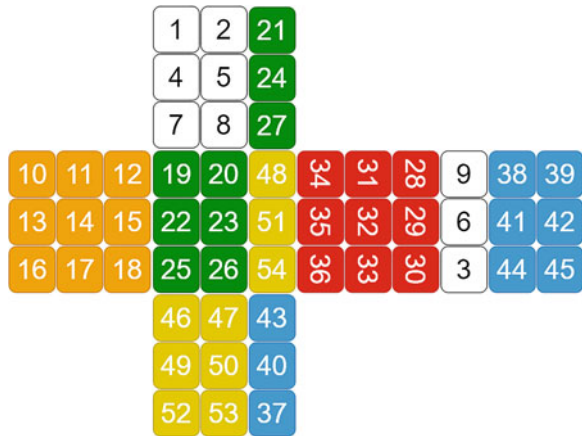
Figure 3.11 shows the spread of a Rubik cube. In this figure, the numbers on the squares show the locations of the fields in the corresponding ordered list.

From a vertical or a horizontal perspective, a Rubik cube consists of three planes that can rotate clockwise or counterclockwise on top of each other. Let us represent the six faces of a Rubik cube by  $F$  (front),  $U$  (up),  $R$  (right),  $B$  (back),  $L$  (left), and  $D$  (down). We can define the 12 basic operations, each of which rotates one of the

**Fig. 3.11** A spread Rubik cube



**Fig. 3.12** A spread Rubik cube after an  $\mathcal{F}$  operation assuming the red face as the front face



faces by  $90^\circ$  clockwise or counterclockwise. We represent the operations of rotating the front face (by  $90^\circ$ ) clockwise and counterclockwise by  $\mathcal{F}$  and  $\mathcal{F}'$ , respectively. Similarly, the operations that rotate other faces are represented by  $\mathcal{U}$ ,  $\mathcal{U}'$ ,  $\mathcal{R}$ ,  $\mathcal{R}'$ ,  $\mathcal{B}$ ,  $\mathcal{B}'$ ,  $\mathcal{L}$ ,  $\mathcal{L}'$ ,  $\mathcal{D}$ , and  $\mathcal{D}'$ . For example, Fig. 3.12 shows the spread of the Rubik cube in Fig. 3.11 after an  $\mathcal{F}$  operation assuming that the red face is the front face. Every other operation can be implemented as a combination of the basic operations.

It can easily be shown that the number of possible patterns for the Rubik cube satisfies Eq. (3.13),

$$P_R = \frac{8! \cdot 12! \cdot 3^8 \cdot 2^{12}}{2 \cdot 3 \cdot 2} = 43252003274489856000. \tag{3.13}$$

A solution to the Rubik cube is a sequence of valid operations that gathers all squares of the some color in the same face. It has been shown that a solution to the Rubik cube consists of  $G_R \leq 20$  face rotation operations (by  $90$  or  $180^\circ$ ) at

a minimum, depending on the initial pattern. The original Rubik cube (invented by Rubik Erno) is a  $3 \times 3 \times 3$  cube. However, a variety of variants have been introduced later.

### 3.6.2.1 Related Problems and Challenges

As suggested by the research literature, the following problems are of important with respect to Rubik's cubes.

- Solving challenge [483–485]
- Training challenge [486, 486, 487]

### 3.6.2.2 Applications in Science and Technology

In recent years, magic cubes have found their applications in several scientific [488] and technological [489] areas.

## 3.7 Cryptography Using Latin/Magic Squares and Cubes

In this section, we discuss the cryptographic properties and applications of Latin and magic squares and cubes.

### 3.7.1 Latin Squares and Cryptography

Latin squares have been used to build improved variants of traditional ciphers [490]. Moreover, they have been used in cryptanalysis as well as the evaluation of cryptosystems [491, 492]. Cryptosystems based upon Latin squares have been used in some real-world technological environments [493].

Latin squares have many cryptographic properties and applications, some of which are discussed below.

**Cryptographic Properties** The reason why Latin squares are of interest to the cryptography research community is their capability of providing the following cryptographic properties.

- Confusion and diffusion [494, 495]
- Chaos [496]

There are numerous cryptographic scenarios that depend on confusion and diffusion [497, 498] as well as chaos [499, 500]. This signifies the role of Latin squares in cryptography.

### 3.7.1.1 Applications in Cryptographic Mechanisms

Latin squares have been used in the following cryptographic mechanisms.

1. Permutation, substitution, and S-boxes [501, 502]
2. Hash functions [503]
3. Cryptographic transformations [504]

**Applications on Different Content Types** Recent research works show that Latin squares can be used to encrypt the following content types.

1. Images ciphers [505, 506] and visual cryptography [507, 508]
2. Text encryption [509, 510]

### 3.7.1.2 Random Latin Square Generation: A Challenging Problem

Generating random Latin squares is one of the most important problems in the field of Latin square-based cryptography [511–514].

### 3.7.1.3 Sudoku: A Popular Extension

Different variants and extensions of Latin squares such as Kenken puzzles [515] have been used in cryptography. However, Sudoku is probably the most common extension of Latin squares. Cryptographic applications of Sudoku can be divided into the following categories.

1. Applications in cryptography
  - Applications in image encryption [516, 517]
  - Applications in key generation [518, 519]
2. Applications in cryptography-related areas

As suggested by existing research works, the following cryptography-related areas can take advantage of the properties of Sudoku.

  - Authentication [520]
  - Data hiding [521–523]
  - Image scrambling [524]
  - Secret sharing [525]

**Latin Squares in the Ecosystem and the Life Cycle of IoT Cryptography** Latin square-based cryptography can be found almost everywhere in the common ecosystem of Fig. 2.1. It has found its applications in several technological environments [526–528]. It has been used in different security-related scenarios [507, 526]. It has also been successfully tested on different content types [528, 529]. Furthermore, Latin square-based cryptography is capable of taking advantage of different enablers

[494, 529, 530]. Moreover, Latin squares-based cryptography plays critical roles in the common life cycle of Fig. 2.2. For example, it is compatible to different design patterns [505, 531]. Moreover, it has been evaluated using different routines [491, 494].

### **3.7.2 *Magic Square and Cryptography***

Similar to the case of Latin squares, magic squares have found their applications in cryptography and related areas. Among these applications, one may refer to the following.

#### **3.7.2.1 Applications in Cryptography**

1. Cryptosystem modeling [532]
2. Image encryption [460]
3. Stream ciphers [533]

#### **3.7.2.2 Applications in Cryptography-Related Areas**

1. Data/signal hiding [534, 535]
2. Authentication [536, 537]

### **3.7.3 *Latin Cube and Cryptography***

To the best of our knowledge, there only a few research works focusing on the applications of Latin cubes in cryptography. Some of these works have investigated the applications of Latin cubes in image encryption [538, 539], random number generation (RNG) [540], etc.

### **3.7.4 *Magic Cube and Cryptography***

Unlike Latin cubes, magic cubes are good choices for application in cryptography. There are several reasons for this popularity. To mention a few, one may refer to the following reasons.

### 3.7.4.1 A Good Scrambling-Based Transformation for Chaotic Encryption

Because of the following applications, magic cubes can be considered as good scrambling-based transformations to be used in chaotic cryptography.

- Applications in scrambling [541, 542]
- Applications in different transformations [543, 544]
- Applications in the creation of chaotic functions [545, 546]

### 3.7.4.2 A Good Choice for Improving Existing Cryptosystems

It was shown in [547] that magic cube can be used to improve the security of existing cryptosystems. Other researchers have been using Rubik cubes for improving some well-known cryptosystems [548, 549].

### 3.7.4.3 Tested on Different Kinds of Contents

Rubik's cubes have been used for encrypting several content types, among which we can mention the following.

- Text [550, 551]
- Binary contents [552]
- Image [553–556]

### 3.7.4.4 Tested in Different Computing Platforms

Cryptosystems based upon magic squares have been examined in different computing platforms. We mention some of these platforms in the following.

- Mobile devices [557]
- Virtual systems [558]
- Cloud storage systems [559]

### 3.7.4.5 Good for Key Management

Magic cubes have been proven good choices for application in key management [560, 561]

### 3.7.4.6 Applications in Cryptography-Related Areas

In addition to cryptography, magic cubes have been used in some related areas including data hiding [562, 563].



# Chapter 4

## Boolean Cryptography



### 4.1 Introduction

Boolean cryptography has been of interest to the research community in recent decades [564–566].

- Boolean Algebra
  - Boolean algebra plays a significant role in Boolean cryptography [567, 568].
  - Boolean Elements
    - \* Boolean predicates
    - \* Boolean matrices
  - Boolean Operations [569]
    - \* Boolean matrix multiplication
- Boolean Functions [570]

Constructing Boolean functions with cryptographic properties is a challenging problem [571].

  - Vectorial Boolean Functions
- Boolean Mappings
- Boolean Maskings [572]

Boolean maskings are used order to protect devices performing cryptographic algorithms against side-channel attacks.
- Boolean Substitution and Permutation
- Boolean Queries Over Encrypted Data

Recent literature comes with several works focusing on queries over different kinds of servers [573] and databases [574]. Many researchers have studied

different aspects of queries over encrypted outsourced and [575] cloud [576, 577] data.

- Boolean Search

Boolean search is a common type of query over encrypted data[578, 579]. Especially, keyword searching is a significant challenge in this area [580] [573].

- Boolean Permutation [581]

- Boolean S-Boxes [582]

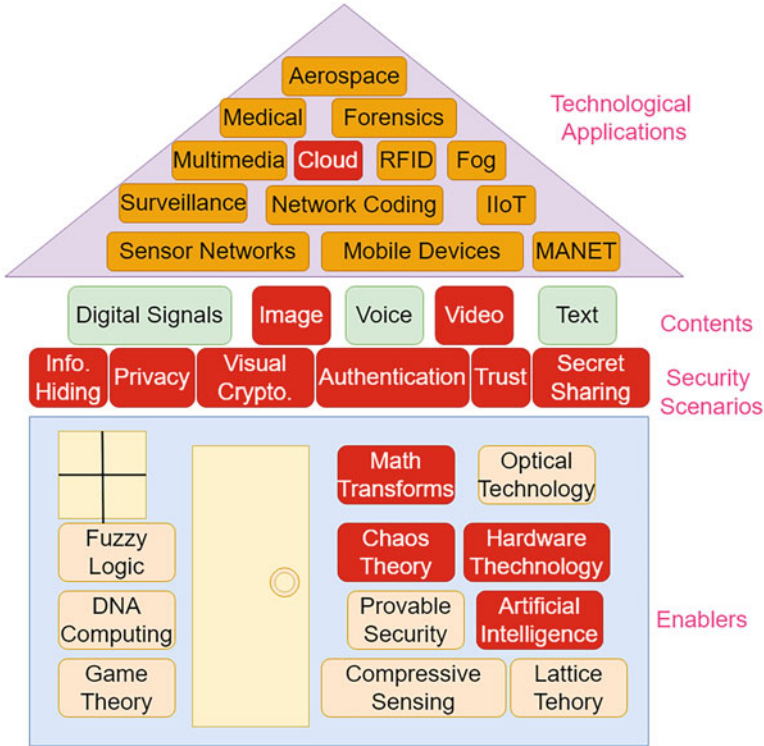
- Boolean Problems

There are a few Boolean problems with applications in cryptography. As an example, one may refer to Boolean Satisfiability Problem [583].

The rest of this chapter is organized as follows. Section 4.2 studies the role of Boolean cryptography in the ecosystem of cryptography (developed in the first part of this book). In this section under this topic, we show that Boolean cryptography is used in the same technological environments as IoT cryptography. Similarly, we highlight the applications of Boolean cryptography in security-related areas connected to IoT cryptography. Moreover, we show that Boolean cryptography can be applied on the content types that need to be processed in IoT cryptography. Section 4.3 connects Boolean cryptography to the life cycle of IoT cryptography. This section shows that the objectives considered in the design of IoT cryptosystems are considered in Boolean cryptography as well. We demonstrate that Boolean cryptography is compatible with the dominating design patterns in IoT cryptography. Moreover, we demonstrate the adaptability of Boolean cryptography with the existing cryptosystems and modern cryptography paradigms, which is a critical need in IoT cryptography. Further, we show how the issues in the implementation phase of IoT cryptography can be resolved using Boolean cryptography. Lastly, we highlight the role of Boolean cryptography in the design phase routines of IoT cryptography, namely, analysis, cryptanalysis, and attack.

## 4.2 The Role in the Ecosystem of Information-Theoretic IoT Cryptography

Boolean cryptography is frequently seen almost everywhere in the ecosystem of information-theoretic IoT cryptography. It has many technological applications in different areas including cloud computing [576] and IoT [584]. Several security-related scenarios can take advantage of Boolean cryptography. Among these scenarios, one may refer to authentication [580], information hiding [585], visual cryptography [569], trust [566, 586], privacy [587, 588], and secret sharing [589, 590]. Boolean methods can be used to encrypt differed content types including image [582, 585, 591] and video [592]. Moreover, different enablers such as



**Fig. 4.1** The position of Boolean cryptography in the ecosystem of information-theoretic cryptography

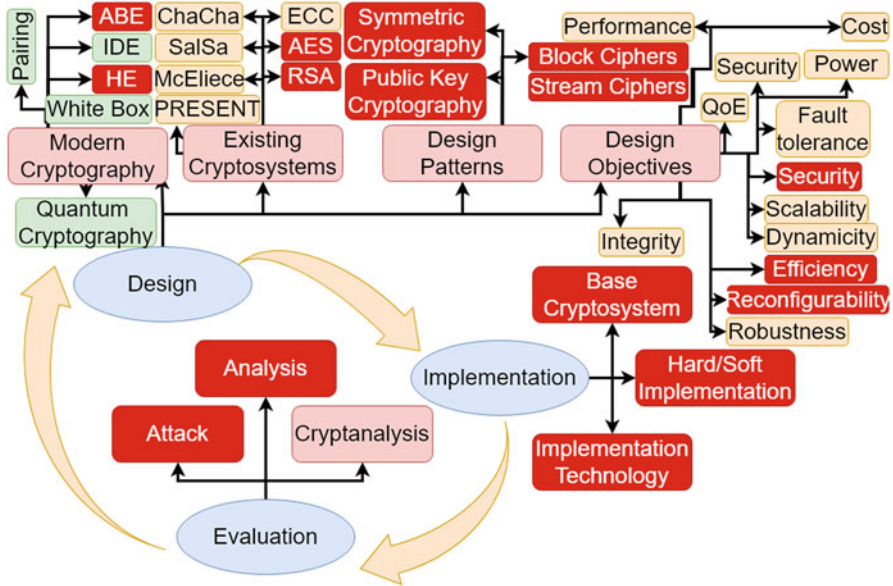
complexity theory [570], artificial intelligence [593, 594], hardware technology [595], mathematical transforms [591], and chaos theory [582] support Boolean cryptography.

According to the above discussions, the position of Boolean cryptography in the ecosystem of information cryptography can be illustrated as shown in Fig. 4.1.

In Fig. 4.1, the rectangles designated by red asterisks show the places, where Boolean cryptography appears as a solution.

### 4.3 The Position in the Life Cycle of Information-Theoretic IoT Cryptography

Similar to the case of the ecosystem, the life cycle of information-theoretic cryptography comes with frequent occurrences of Boolean cryptography. Researchers have worked on the design, implementation, and evaluation of cryptosystems via Boolean approaches. Various objectives have been considered in the design of cryptosystem,



**Fig. 4.2** The position of Boolean cryptography in the life cycle of information-theoretic cryptography

among which we can mention security [577], efficiency [578], and reconfigurability [596]. Boolean cryptography has been proven to be flexible to different design patterns, such as symmetric cryptography [597], public key cryptography [583, 598], stream ciphers [596, 599], and block ciphers [592]. Existing cryptosystems including AES [600] and RSA [601] have been used to design Boolean cryptographic systems. Boolean cryptography has exhibited its efficiency in modern cryptography paradigms, such as homomorphic encryption (HE) [578, 579] and attribute-based encryption (ABE) [602]. Moreover, different challenges have been investigated in the implementation phase of Boolean cryptography. These challenges include the choice among base cryptosystems [603, 604], hardware/software implementation approaches [596, 605], and implementation technologies [568]. Furthermore, several routines including analysis [578, 605] and attack [578, 606] have been studied in the implementation phase of Boolean cryptography.

The position of Boolean cryptography in the life cycle of information cryptography can be illustrated as shown in Fig. 4.2.

In Fig. 4.2, the rectangles highlighted in red show the places, where Boolean cryptography appears as a solution.

# Chapter 5

## A Hybrid Combinatorial-Boolean Approach Toward Perfect Secrecy in IoT



### 5.1 Introduction and Basic Concepts

Shannon discussed the security of a cryptosystem from the viewpoint of information theory, which is considered a foundational treatment of modern cryptography [607]. Perfect secrecy states that no information of the probability distribution of plain text can be gained when the probability distribution of cipher text is known. Let  $S$  be a cryptosystem whose plain text and cipher text sets (finite) are  $\mathcal{P}$  and  $\mathcal{C}$ , respectively. Suppose  $Pr[x]$  and  $Pr[x/y]$  are the probability of occurring  $x$  and the conditional probability of  $x$  given  $y$ , respectively,  $x \in \mathcal{P}$  and  $y \in \mathcal{C}$ . From a statistical perspective, perfect secrecy of a cryptosystem is formally defined as follows.

**Definition 5.1** A cryptosystem has perfect secrecy or equivalently it is perfectly secure if  $Pr[x/y] = Pr[x]$  for all  $x \in \mathcal{P}$  (plain text) and  $y \in \mathcal{C}$  (ciphertext).

Shannon demonstrated that key-dependent perfect secrecy requires a secret key that is not shorter than the plain text [607]. This keeps perfect secrecy from being widely implemented in real-world applications despite its intriguing advantages. One-time pad (OTP) is the only real-world implementation of perfect secrecy seriously studied by the research community and used by the industry. In OTP, the transmission of every individual message requires a new random key to be generated.

In this chapter, we revisit perfectly secure cryptography in real-time, resource-constrained IoT systems via investigating the possibility of secret algorithm perfect secrecy. Our proposed approach is based on a combinatorial square design named Latin square and a class of Boolean functions referred to as resilient functions.

In our approach, perfect secrecy can be achieved using a secret key and/or a secret algorithm. From a theoretical point of view, the first challenge in secret algorithm perfectly secure cryptography is the lack of systematic methods for creating cryptographic algorithms, which are theoretically guaranteed to be perfectly secure.

A solution to this problem is presented in this chapter. The solution is based on a framework for exhaustively creating and encoding all theoretically possible perfectly secure cryptographic algorithms.

In this chapter, we first model a general cryptosystem as a set of reversible  $(n, n)$ -functions, one of which is chosen based on the key value. We use this model to calculate the number of all cryptographic algorithms, which can theoretically exist. Since the calculated number is very huge, we argue that we can depend on secret algorithms instead of or in addition to secret keys. This leads to the notion of secret algorithm cryptography. We also calculate the minimum average code length for encoding reversible  $(n, n)$ -functions (Sect. 5.1.3). Then, we propose an encoding scheme, which assigns minimum-length codes to reversible Boolean functions. Next, we model the set of perfectly secure cryptographic algorithms as a super set of  $n$ -resilient  $(n, n)$ -functions. We also propose a procedure that guarantees exhaustive creation of all theoretically-possible perfectly secure cryptographic algorithms. Moreover, we calculate the number of these algorithms and prove it to be very huge. We use this calculation to obtain an upper bound of the number of  $n$ -resilient  $(2n, n)$ -functions. In addition, we calculate the minimum average code length for encoding each perfectly secure cryptographic algorithm. Moreover, we propose an encoding scheme, which assigns a unique minimum-length code to every individual perfectly secure algorithm. The construction procedure, the encoding scheme and the calculations form the basis of a cryptographic scheme that partially depends on secret algorithms. Next, we take one step forward and propose another perfectly secure cryptographic scheme that depends only on secret algorithms without the use of any secret key. We refer to this scheme as secret algorithm cryptography. Finally, the relation between perfect secrecy and secret algorithm cryptography is established by proving a theorem stating that the secret algorithm cryptography presented in this chapter is perfectly-secure.

### ***5.1.1 Motivations, Novelties, and Achievements***

To the best of our knowledge, there is no research work focusing on secret algorithm perfect secrecy in IoT. This is despite the advantages of perfect secrecy as well as resource constraints in IoT-based systems along with the intensive amounts of computation needed by key generation and exchange mechanisms. These shortcomings motivate us to investigate challenges and requirements of secret algorithm perfectly secure cryptography in IoT. More specifically, there are some shortcomings in existing research, works which motivate our work in this table. Among these shortcomings, we can mention the following.

- There is no systematic method for generating a perfectly secure algorithm.
- There is no idea regarding the number of theoretically possible perfectly secure algorithms.

- There is no specific method for the specification and numerical encoding of such algorithms.
- There is no secret algorithm method in the literature for perfectly secure cryptography.

In the next sections of this chapter, we are going to address the above problems.

The novelties and the achievements of our work in this chapter are as follows.

1. In this chapter, we present the first hybrid combinatorial-Boolean approach toward perfect secrecy in IoT environments.
2. We present perfectly secure cryptographic algorithms using resilient Boolean functions for the first time.
3. We present the first systematic framework for creating, counting, and encoding all theoretically possible perfectly secure cryptographic algorithms.
4. We propose the first secret algorithm perfectly secure method.
5. We obtain an upper bound for the number of  $n$ -resilient  $(2n, n)$ -functions.
6. As side achievements, we present the first methods for the encoding Latin squares and the random generation of perfectly secure algorithms.

Figure 5.1 illustrates the proposed approach, its interactions with Latin squares and perfectly secure algorithms, and its achievements.

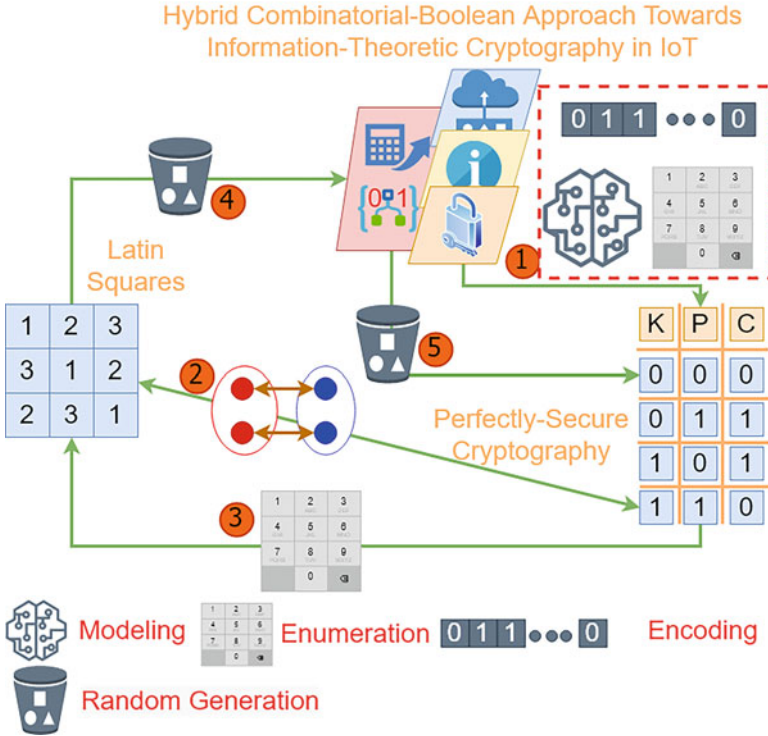
### 5.1.2 Organization

The rest of this chapter is organized as follows. Section 5.1.3 presents some basic definitions and preliminary discussions needed before introducing the proposed approach. Section 5.2 introduces the proposed approach. Section 5.2.2 presents the representation, encoding, and enumeration schemes for generic cryptographic algorithms. Section 5.2.2.4 present the same schemes for perfectly secure cryptographic algorithms. This subsection connects perfectly secure cryptographic algorithms to Latin square using a one-to-one mapping and uses the properties of Latin squares to present the random algorithm cryptography method. Section 5.3 presents the reasons why the proposed approach is the proper application for IoT environments.

### 5.1.3 Definitions and Preliminary Discussions

In this section, we are going to present some definitions needed throughout the chapter and make some preliminary discussions.

Let  $\mathbb{F}_2$  be a binary field and  $\mathbb{F}_2^n = \{\mathbf{x} = (x_1, x_2, \dots, x_n) : x_i \in \mathbb{F}_2, 1 \leq i \leq n\}$ . A function  $f$  from  $\mathbb{F}_2^n$  to  $\mathbb{F}_2$  is said to be an  $n$ -variable Boolean function, and the set of all  $n$ -variable Boolean functions is denoted by  $\mathcal{B}_n$ . A Boolean function  $f \in \mathcal{B}_n$  is balanced if its truth table contains an equal number of 1s and 0s. A function



**Fig. 5.1** The proposed approach: interactions with Latin squares and perfectly secure algorithms, and achievements

$g : \mathbb{F}_2^n \rightarrow \mathbb{F}_2^m$  is said to be vectorial Boolean function and also called  $(n, m)$ -function. An  $(n, m)$ -function  $f$  is said to be balanced if the cardinality of the sets  $f^{-1}(\mathbf{y})$  is equal to  $2^{n-m}$  for all  $\mathbf{y} \in \mathbb{F}_2^m$ . An  $(n, n)$ -function  $g$  is said to be reversible (or bijective) if it is both injective and surjective. A reversible vectorial Boolean function with  $n$  inputs and  $n$  outputs is referred to as an  $(n, n)_{\mathcal{R}}$ -function in this chapter. It is well-known that the cardinality of the set of all  $(n, n)_{\mathcal{R}}$ -functions is equal to  $2^n!$ .

For an unsigned binary string  $b$ ,  $Dec(b)$  is defined as the decimal equivalent of  $b$ . On the other hand, for a decimal integer  $i, 0 \leq i \leq 2^n - 1$ ,  $Bin(i, n)$  is defined as the unsigned  $n$ -bit binary string equivalent to  $i$ . We also define  $V(n)$  as  $V(n) = [v_{i \in [0, 2^n - 1]} = Bin(i, n)]$  Also for a vector  $V$ ,  $length(V)$  is defined as the number of the elements in the vector. Moreover, for a vector  $V$  and a set  $S$ ,  $V/S$  is defined as a vector, which results if we remove elements of  $S$  from  $V$ . Thus, if  $length(V) = l$  and  $r$  of  $V$  elements are elements of  $S$  as well,  $V/S$  will include  $l - r$  elements.



### 5.1.4 Resilient Functions

A Boolean function  $f \in \mathcal{B}_n$  has  $\alpha$ -correlation immunity (correlation immunity of order  $\alpha$ ) if its values are statistically independent of any subset of  $\alpha$  input variables.

**Definition 5.2** An  $n$ -variable Boolean function  $f$  is said to be resilient of order  $\alpha$  (or  $\alpha$ -resilient) if  $f$  is balanced and correlation immune of order  $\alpha$ , i.e., a Boolean function is  $\alpha$ -resilient if on fixing any  $k$  coordinates,  $0 \leq k \leq \alpha$ , the restricted functions are all balanced.

The resilient  $(n, m)$ -function of  $\alpha$ th order is defined by the following way.

**Definition 5.3** Let  $n, m$ , and  $\alpha$  be positive integers with  $0 \leq \alpha \leq n$ , and  $f$  be an  $(n, m)$ -function. Then,  $f$  is called  $\alpha$ th order correlation immune if its output distribution does not change when at most  $\alpha$  coordinates in inputs are kept constant. It is called  $\alpha$ -resilient if it is balanced and  $\alpha$ th order correlation immune, that is, if it stays balanced when at most  $\alpha$  coordinates in inputs are kept constant.

When a Boolean function is to be used in a cryptosystem, it is required that the output of the Boolean function should not be correlated with a subset of input variables. In other words, the function needs to resist the correlation attack [608]. The concept of resiliency of has been introduced to address such kind of resistance. Resilient functions play a significant role in cryptosystems. Therefore, they have appeared in many research works in this area. For instance, Siegenthaler [608] showed that for an  $n$ -variable, Boolean function of degree  $r$  and resiliency of order  $\alpha$  satisfied the inequality  $\alpha + r \leq n - 1$ , which is called Siegenthaler's inequality. Sarkar and Maitra [609, 610] also derived many results regarding the relation between the nonlinearity and the order of resiliency of a Boolean function. Further many highly significant cryptographic Boolean functions were constructed using resilient functions (see [611–615] and the references therein).

We refer to an  $\alpha$ -resilient  $(n, m)$ -function by an  $(n, m, \alpha)$ -function. Let us consider  $n = m + \alpha$  and  $f$  is an  $(n, m, \alpha)$ -function. Then, if we fixed any  $\alpha$  input coordinates, the restricted function is reversible (or balanced) and these restricted functions can be consider as an  $(m, m)$ -function, which are reversible.

## 5.2 The Proposed Approach

In this section, we first introduce the notion of secret algorithm cryptography and then present our approach for secret algorithm perfect secrecy in IoT.

### 5.2.1 A Look at Secret Algorithm Cryptography

Kerckhoffs's principle states that in a key-based cryptosystem, the algorithm should be exposed and the key should be kept secret. With the emergence of secret algorithm cryptography, this principle will no longer be considered as an axiom in secret algorithm cryptography. *Key-dependent algorithm cryptosystems* a.k.a. *secret algorithm cryptosystems* or *random algorithm cryptosystems* have been of interest to the research community in recent years [616, 617]. In a secret algorithm cryptosystem, the encryption and decryption algorithms' configurations are functions of the secret key. In such an algorithm, (part of) the secret key is used for random (secret) configuration of the algorithm in addition to the part directly combined with the plain text.

Figure 5.2 compares key-dependent algorithm cryptography with traditional cryptography.

secret algorithm cryptosystems have been tested under different attacks [618]. They have been used in different technological environments, such as sensor networks [619] and IoT [620, 621]. These algorithms have been applied on different content types [622]. The literature suggests key-dependent algorithm cryptosystems as a good choice, especially for lightweight cryptography [617, 620]. Some well-known cryptosystems have been modified to achieve key-dependent variants [623, 624].

Researchers have studied different elements of cryptographic algorithms to evaluate the impact of their dependence on the key. Among these elements,

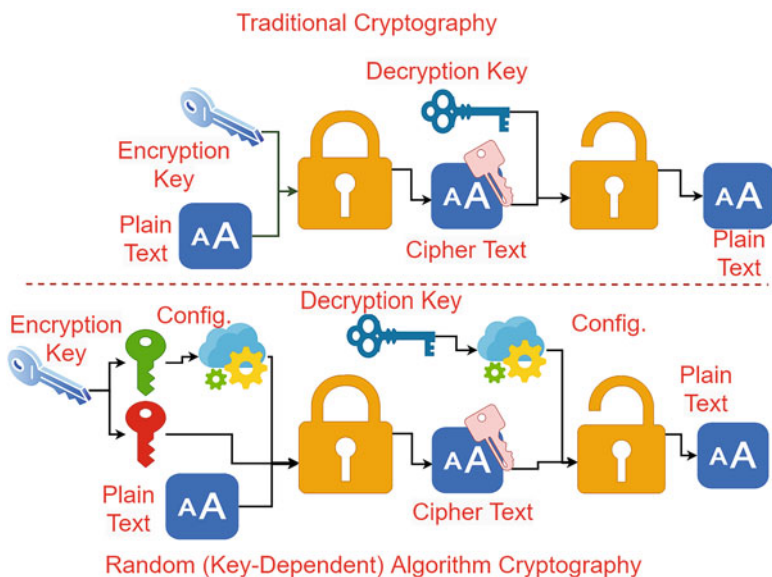


Fig. 5.2 Key-dependent algorithm cryptography versus traditional cryptography

one may refer to feedback configuration matrices [625], substitution boxes (S-boxes) [626–628], permutation boxes (P-boxes) [620, 629], linear-feedback shift registers (LFSRs) [620], and mathematical transforms [622]. Different kinds of cryptographic algorithms such as block [626] and stream ciphers [620] as well as symmetric and public key cryptography [630] have been used for this purpose.

## 5.2.2 *Generic Cryptographic Algorithms: Representation, Encoding, and Enumeration*

In this subsection, we present our presentation as well as our enumeration and encoding schemes for generic cryptographic algorithms.

### 5.2.2.1 Representation

In the following, we use the properties of  $(n, n)_{\mathcal{R}}$ -functions to represent a general cryptographic algorithm. Next, we show the relation between cryptographic algorithms and resilient vectorial Boolean functions. Then we calculate the number of all theoretically possible cryptographic algorithms. We use the latter calculations to justify the concept of secret algorithm cryptography.

The following remark shows the relation between  $(n, n)_{\mathcal{R}}$ -functions and  $(k, n)$ -algorithms, an algorithm with  $k$  key bits,  $n$  plain text, and cipher text bits. It is clear that a generic cryptographic algorithm, which is not necessarily perfectly-secure, can be represented by a  $(k, n)$ -algorithm, where  $k$  is the length of the key and  $n$  is the length of the plain text.

*Remark 5.1* A general  $(k, n)$ -algorithm can be modeled by a set of  $2^k$   $(n, n)_{\mathcal{R}}$ -functions, one of which is selected according to the fixed value of the key.

The above remark is obvious because a cryptographic algorithm should be reversible given the key.

### 5.2.2.2 Encoding

Every  $(n, n)_{\mathcal{R}}$ -function can obviously be encoded by  $n \cdot 2^n$  bits. To do this, we can simply concatenate the output strings in each reversible function to make a numeric code for that function. But the following theorem states that we should be able to encode  $(n, n)_{\mathcal{R}}$ -function by shorter code lengths.

**Theorem 5.1** *The minimum average code length required to encode all permutations of  $V(n)$  is above bounded by  $(n - 1)2^n + 1 < n \cdot 2^n$ .*

**Proof** Since the total number of permutations on  $V(n)$  is  $2^n!$ , we should be able to encode them with an average code length of  $\log_2(2^n!)$ . The minimum average code length will be obtained from the following equation.

$$\begin{aligned}
\bar{L} &= \lceil \log_2(2^n!) \rceil \\
&= \lceil \log_2(2^n \cdots (2^{n-1} + 1)2^{n-1}(2^{n-1} - 1) \cdots 2 \cdot 1) \rceil \\
&= \left\lceil \log_2 \left( \prod_{i=1}^n \prod_{j=2^{i-1}+1}^{2^i} j \right) \right\rceil \\
&= \left\lceil \sum_{i=1}^n \log_2 \left( \prod_{j=2^{i-1}+1}^{2^i} j \right) \right\rceil \\
&= \left\lceil \sum_{i=1}^n \sum_{j=2^{i-1}+1}^{2^i} \log_2(j) \right\rceil.
\end{aligned}$$

It is obvious that

$$\begin{aligned}
\bar{L} &< \sum_{i=1}^n \sum_{j=2^{i-1}+1}^{2^i} \lceil \log_2(j) \rceil \\
&= \sum_{i=1}^n i \cdot 2^{i-1} = (n-1)2^n + 1.
\end{aligned}$$

□

In fact, since the total number of  $(n, n)\mathcal{R}$ -functions is  $2^n!$ , we should be able to encode each of them by a minimum average code length of  $\log_2(2^n!)$ .

If we chose an encoding scheme with average code length of  $L > \log_2(2^n!)$ , there will be  $2^L - \log_2(2^n!)$  invalid codes. Thus, it is important to design an encoding scheme with the minimum possible average code length. The following theorem introduces our proposed encoding scheme. We will show later that the minimum average code length is met by this encoding scheme.

**Algorithm 5.1**  $PC = \text{PermutationCode}(Y)$

Begin

Set  $PC = 0$ .

For  $i$  in  $[0, 2^n - 2]$

Set  $S_i = 0$ .

For  $j$  in  $[i + 1, 2^n - 1]$

If  $y_j < y_i$

Set  $S_i = S_i + 1$ .

Set  $PC = PC + S_i \cdot (2^n - (i + 1))!$ .

End

**Theorem 5.2** *Algorithm 5.1 can assign a unique numeric code in  $[0, n! - 1]$  to every individual permutation  $\pi$  of  $X = [x_{i \in [0, n-1]} = i]$ , where  $[0, m] = \{0, 1, \dots, m\}$  for any positive integer  $m$ .*

**Proof** Algorithm 5.1 creates different codes for different permutations. The reason is that  $S \cdot (n - (j + 1))!$  is always smaller than  $(n - (i + 1))!$  if  $j > i$ , and this results the fact  $S$  is smaller than  $n - i$  for every  $j \in [i + 1, n - 1]$  if  $S_i > 0$ . Therefore, the Algorithm 5.1 assigns  $2^n!$  distinct codes to  $2^n!$  distinct permutations. Moreover, the above algorithm assigns the smallest code (0) to  $[0, 1, \dots, n - 1]$  and assigns the greatest code  $(n! - 1)$  to  $[n! - 1, n! - 2, \dots, 0]$ . Thus, the codes assigned to the permutations by this algorithm will be in  $[0, n - 1]$ .  $\square$

**Lemma 5.1** *Algorithm 5.1 assigns codes of length  $\lceil \log_2(2^n!) \rceil$  to permutations of  $V(n)$ .*

**Proof** Since the total number of codes assigned by the Algorithm 5.1 is equal to  $2^n!$ , they can be assigned codes of length  $\lceil \log_2(2^n!) \rceil$ .  $\square$

Table 5.1 shows the codes assigned by our proposed scheme to all  $(2, 2)_R$ -functions.

### 5.2.2.3 Enumeration

**Lemma 5.2** *The number of all  $(k, n)$ -algorithms is equal to*

$$\frac{(2^n!)!}{(2^n! - 2^k)!}$$

**Proof** The total number of  $(n, n)_R$ -functions is  $2^n!$ , and  $2^k$  of them is collected in a  $(k, n)$ -algorithm. Thus, the total number of  $(k, n)$ -algorithms is equal to  $\frac{(2^n!)!}{(2^n! - 2^k)!}$ .  $\square$

The above lemma states that there can be a huge number of cryptographic algorithms. The idea of secret-key cryptography comes up here. In fact, keeping the algorithm confidential can make the cryptosystem harder-to-break from computational point of view. The problem here is that some of these algorithms may not satisfy extra criteria, such as resistance to different kinds of attacks. Therefore, we propose to focus only on perfectly secure algorithms discussed in the next section.

**Table 5.1** Codes assigned to  $(2, 2)_{\mathcal{R}}$ -functions

Algorithm	$\mathcal{P}$	$\mathcal{C}$	Algorithm	$\mathcal{P}$	$\mathcal{C}$	Algorithm	$\mathcal{P}$	$\mathcal{C}$
00000	00	00	01000	00	01	10000	00	10
	01	01		01	10		01	11
	10	10		10	00		10	00
	11	11		11	11		11	01
00001	00	00	01001	00	01	10001	00	10
	01	01		01	10		01	11
	10	11		10	11		10	01
	11	10		11	00		11	00
00010	00	00	01010	00	01	10010	00	11
	01	10		01	11		01	00
	10	01		10	00		10	01
	11	11		11	10		11	10
00011	00	00	01011	00	01	10011	00	11
	01	10		01	11		01	00
	10	11		10	10		10	10
	11	01		11	00		11	01
00100	00	00	01100	00	10	10100	00	11
	01	11		01	00		01	01
	10	01		10	01		10	00
	11	10		11	11		11	10
00101	00	00	01101	00	10	10101	00	11
	01	11		01	00		01	01
	10	10		10	11		10	10
	11	01		11	01		11	00
00110	00	01	01110	00	10	10110	00	11
	01	00		01	01		01	10
	10	10		10	00		10	00
	11	11		11	11		11	01
00111	00	01	01111	00	10	10111	00	11
	01	00		01	01		01	10
	10	11		10	11		10	01
	11	10		11	00		11	00

#### 5.2.2.4 Perfectly Secrecy: Representation, Encoding, and Enumeration

We refer to a perfectly secure encryption algorithm with  $k$  key bits,  $n$  plain text bits, and  $n$  cipher text bits as a  $(k, n)_{\mathcal{PS}}$ -algorithm. According to Shannon's perfect-secrecy theory, a necessary criterion for perfect secrecy is that the length of the key should be equal to or greater than that of the plain text. Since long keys are difficult to create, exchange, and manage, we will focus on the shortest possible key length, i.e., we will focus on  $(n, n)_{\mathcal{PS}}$ -algorithm.

**Table 5.2** A  $\mathcal{PS}$ -type truth table  $T$  for  $n = 2$ 

Key	Plain text	Cipher text	Functions
00	00	11	$f_0$
00	01	01	
00	10	00	
00	11	10	
01	00	01	$f_1$
01	01	00	
01	10	10	
01	11	11	
10	00	00	$f_2$
10	01	10	
10	10	11	
10	11	01	
11	00	10	$f_3$
11	01	11	
11	10	01	
11	11	00	

In this section, we propose a perfectly secure cryptographic scheme, which uses secret keys as well as secret algorithms. But before beginning our discussions in this section, we need to present some definitions. A  $\mathcal{PS}$ -type truth table  $T$  is defined as a truth table with  $3n$  columns (each  $n$  for the key, plain text, and cipher text) and  $2^{2n}$  rows (for  $2n$  bits including the key and plain text). The first  $2n$  columns in a  $\mathcal{PS}$ -type truth table are considered already filled with the list of  $2^{2n}$  possible  $2n$ -bit values in a natural ascending order of first  $n$  bits. A  $\mathcal{PS}$ -type truth table  $T$  is divided into  $2^n$  blocks each containing  $2^n$  rows. The blocks are represented by  $b_0, b_1, \dots, b_{2^n-1}$ , say. The  $j$ th row of  $b_i$  block is represented by  $b_{i,j}$ . We denote the key part of  $b_{i,j}$  by  $b_{i,j,0}$ , the plain text part by  $b_{i,j,1}$ , and the cipher text part by  $b_{i,j,2}$ . Thus, in a  $\mathcal{PS}$ -type truth table  $T$ , after filling inside  $b_{i,j}$  every  $i, j \in \{0, 1, \dots, 2^n - 1\}$ , every block will contain an  $(n, n)$ -function. For example, a  $\mathcal{PS}$ -type truth table  $T$  for  $n = 2$  is represented as in Table 5.2.

### 5.2.2.5 Representation

*Remark 5.2* An  $(n, n)_{\mathcal{PS}}$ -algorithm can be represented by a set of  $2^n$   $(n, n)_{\mathcal{R}}$ -functions selected by a  $n$ -length key, in which the perfect secrecy criterion is satisfied.

The following lemma builds the relation between the set of  $(2n, n, n)$ -functions and the set of  $(n, n)_{\mathcal{PS}}$ -algorithms.

**Lemma 5.3** *Let  $n$  be a positive integer. If a  $(2n, n)$ -function  $f$  is  $n$ -resilient, then  $f$  is an  $(n, n)_{\mathcal{PS}}$ -algorithm.*

**Table 5.3** A  $(2, 2)_{\mathcal{PS}}$ -algorithm not consisting of  $(4, 2, 2)$ -functions

Key	Plain text	Cipher text
00	00	00
00	01	10
00	10	01
00	11	11
01	00	01
01	01	11
01	10	10
01	11	00
10	00	11
10	01	01
10	10	00
10	11	10
11	00	10
11	01	00
11	10	11
11	11	01

**Proof** Suppose  $f$  is a  $(2n, n)$ -function, which is  $n$ -resilient. So fixed first  $n$  bits, the restricted function is balanced and we can consider as a  $(n, n)_{\mathcal{R}}$ -function. Suppose all the restricted functions are denoted by  $f_0, f_1, \dots, f_{2^n-1}$ , and  $f_i$  are reversible, for all  $0 \leq i \leq 2^n - 1$ . If possible, let there exist  $i_0 \neq j_0$  and  $\mathbf{x} \in \mathbb{F}_2^n$  such that  $f_{i_0}(\mathbf{x}) = f_{j_0}(\mathbf{x})$ . Then, we fixed this bit pattern, and the restricted function is not balanced as this restricted function have at least two same output, which is same as  $f_{i_0}(\mathbf{x})$ . Thus, all the restricted functions satisfy that  $f_i(\mathbf{x}) \neq f_j(\mathbf{x})$ , for all  $\mathbf{x} \in \mathbb{F}_2^n$  and  $0 \leq i \neq j \leq 2^n - 1$ , so we get our claim.  $\square$

The converse of the Theorem 5.3 is not true in general. For example, let  $n = 2$ ; then, the algorithm defined as in Table 5.3 is a  $(2, 2)_{\mathcal{PS}}$ -algorithm but not 2-resilient  $(4, 2)$ -function.

### 5.2.2.6 Enumeration and Encoding

Now, we present a procedure for creating  $(n, n)_{\mathcal{PS}}$ -algorithms through calling a recursive algorithm. The procedure is followed by a theorem, which proves that all  $(n, n)_{\mathcal{PS}}$ -algorithms are exhaustively create by the procedure.

#### Procedure 5.1 Create- $\mathcal{PSP}(n)$

Begin

Set  $E = [e_{i,j \in [0, 2^n - 1]} = \emptyset]$  where  $\emptyset$  indicates an empty set.

Set  $M = [m_{i,j \in [0, 2^n - 1]} = V(n)]$ .

Set  $R = V(n)$ .

Set  $A = \emptyset$ .

Set  $z = 0$ .



```

    Set  $r = 0$ .
    Set  $Code = 0$ .
     $\mathcal{PSP}(t)$ .
End.

```

In the above procedure,  $\mathcal{PSP}(t)$  is a recursive algorithm described as follows.

**Algorithm 5.2**  $\mathcal{PSP}(r)$

```

Begin
If  $t == 2^n - 1$ 
    For  $b \in [0, 2^n - 1]$  Do
        Set  $b_{b,r,2}(T) = M(b, r, 1)$ .
        Set  $E(b, r) = E(B, t) \cup M(b, r, 0)$ .
        Set  $M(b, r) = R/E[i]$ .
    Set  $A = A \cup (T, Code)$ .
    Set  $Code = Code + 1$ .
Else
    Allocate  $T$  as a new  $\mathcal{PS}$ -type truth table.
    While  $length(M(b, r))! = 0$ 
        For  $b \in [0, 2^n - 1]$  Do
            Set  $b_{b,r,2}(T) = M(b, r, 1)$ .
            Set  $E(b, r) = E(b, r) \cup M(b, r, 0)$ .
            Set  $M(b, r) = R/E(b, r)$ .
            For  $g \in [r + 1, 2^n - 1]$  Do
                Set  $E(b, g) = E(b, g) \cup M(b, r, 0)$ .
                Set  $M(b, g) = RR/E(b, g)$ .
            For  $g \in [b + 1, 2^n - 1]$  Do
                Set  $E(g, r) = E(g, r) \cup M(b, r, 0)$ .
                Set  $M(g, r) = RR/E(g, r)$ .
         $\mathcal{PSP}(t + 1)$ 
End

```

**Theorem 5.3** *Procedure 5.1 exhaustively creates all possible  $(n, n)_{\mathcal{PS}}$ -algorithms and assigns a unique code to each of them.*

**Proof** The proof of this theorem consists of two parts. In the first part, we need to prove that every  $(n, n)$ -algorithm created by Procedure 5.1 is a  $(n, n)_{\mathcal{PS}}$ -algorithm. The second part should prove that every theoretically possible  $(n, n)_{\mathcal{PS}}$ -algorithm is created and stored by the Algorithm 5.2. To prove the first part, we note that algorithm  $\mathcal{PSP}$  fills  $\mathcal{PS}$ -type truth tables, each with  $2^n \cdot 2^n = 2^{2n}$  empty cells. It keeps a list of values allowed to be inserted into  $b_{b,r,2}(T)$  in  $M(b, r)$  for every  $b, r \in [0, 2^n - 1]$ . When the algorithm starts working, it assumes that  $b_{b,r,2}(T) = V(n)$  for every  $b, r \in [0, 2^n - 1]$ . Upon inserting any value in  $b_{b,r,2}(T)$ , the inserted value is removed from  $M(b, r)$ ,  $M([b + 1, 2^n - 1], r)$ , and  $M(b, [r + 1, 2^n - 1])$ . This guarantees the two following clauses.

- $\forall b \in [0, 2^n - 1], \nexists r_1, r_2 \in [0, 2^n - 1] : r_1 \neq r_2, b_{b,r_1,2}(T) = b_{b,r_2,3}(T)$ .

- $\forall r \in [0, 2^n - 1], \nexists b_1, b_2 \in [0, 2^n - 1] : b_1 \neq b_2, b_{b_1, r, 2}(T) = b_{b_2, r, 3}(T)$ .

Since the number of the blocks and the number of rows in each block are both equal to  $2^n$ , the above two clauses together state that each block in table  $T$  will contain a reversible  $(n, n)$ -function different from those in other blocks. Thus, every filled table  $T$  will be a  $(n, n)_{\mathcal{PS}}$ -algorithm. They also state that  $\forall x \in V(n) : Pr(\mathcal{P} = x/C = c) = Pr(\mathcal{P} = x)$ , i.e., every table  $T$  filled by the algorithm contains a  $(n, n)_{\mathcal{PS}}$ -algorithm. Moreover, in order to prove the second part of the theorem, we note that each run of algorithm  $\mathcal{PSP}$  guarantees to fill  $b_{b, r, 2}(T)$  with every  $V(n)$  element, except for those inserted in previous rows in the same block or the same row in previous blocks. Thus, the algorithm guarantees to create every possible  $(n, n)_{\mathcal{PS}}$ -algorithm.  $\square$

The following theorem calculates the number of all  $(n, n)_{\mathcal{PS}}$ -algorithms. This will help us calculate the minimum average code length required to encode them. We also make use of this calculation to justify the use of secret algorithms.

**Theorem 5.4** *The number of all  $(n, n)_{\mathcal{PS}}$ -algorithms is equal to  $\prod_{i=0}^{2^n-1} (2^n - i)^{i+1}$ .*

**Proof** The number of reversible  $(n, n)$ -functions, which can be inserted in  $b_0(T)$ , is obviously equal to  $2^n!$ . The number of allowable values for every  $b_{1, j}(T)$  reduces by one after filling  $b_0(T)$ , except for  $b_{1, 2^n-1}(T)$  for which there still remains one allowable value. Thus, the number of functions, which can be stored to  $b_0(T)$ , is equal to  $(2^n - 1)!$ . Through a similar reasoning, it can be shown that the number of functions allowable to be stored in  $b_r(T)$  will be equal to  $(2^n - r)!$  for every  $b \in [0, 2^n - 1]$ . Therefore, the total number of  $(n, n)_{\mathcal{PS}}$ -algorithms, each of which is generated by Procedure Create- $\mathcal{PSP}(n)$ , is equal to  $P_s = \prod_{i=0}^{2^n-1} (2^n - i)! = \prod_{i=0}^{2^n-1} (2^n - i)^{i+1}$ .  $\square$

The huge number calculated by Theorem 5.4 makes it theoretically justifiable to keep the algorithm secret in order to achieve larger search space. From Lemma 5.3 and Theorem 5.4, we get the next results.

**Corollary 5.1** *The number of  $n$ -resilient  $(2n, n)$ -function is bounded above by the cardinality of the set  $(n, n)_{\mathcal{PS}}$ -algorithm, i.e.,  $\prod_{i=0}^{2^n-1} (2^n - i)^{i+1}$ .*

Every  $(n, n)_{\mathcal{PS}}$ -algorithm can obviously be encoded by  $n \cdot 2^n \cdot 2^n = n \cdot 2^{2n}$  bits. On the other hand, Theorem 5.4 states that we should be able to encode such an algorithm by an average code length of  $\log_2 \left( \prod_{i=0}^{2^n-1} (2^n - i)^{i+1} \right)$ . The following theorem shows that the minimum average code length here should be less than  $n \cdot 2^{2n}$ .

**Theorem 5.5** *The minimum average code length for encoding  $(n, n)_{\mathcal{PS}}$ -functions is above bounded by*

$$L_m^R = \frac{11 + 3(n^2 - 2^{n+1}) + 3n(n + 3)2^n - (3n - 1)2^{2n}}{6}.$$

**Proof** From Theorem 5.4, we know that the number of all  $(n, n)_{\mathcal{PS}}$ -algorithms is equal to  $\prod_{i=0}^{2^n-1} (2^n - i)^{i+1}$  and

$$\begin{aligned} & \left[ \log_2 \left( \prod_{i=0}^{2^n-1} (2^n - i)^{i+1} \right) \right] \\ &= \left[ \sum_{i=0}^{2^n-1} (i+1) \log_2 (2^n - i) \right] \\ &= \left[ \sum_{t=0}^{2^n-1} (2^n - t + 1) \log_2 t \right] \\ &= \left[ \sum_{t=1}^n \sum_{r=2^{t-1}+1}^{2^t-1} (2^n - r + 1) \log_2 r \right] \end{aligned}$$

It is obvious that

$$\begin{aligned} & \left[ \sum_{t=1}^n \sum_{r=2^{t-1}+1}^{2^t-1} (2^n - r + 1) \log_2 r \right] \\ & \leq \sum_{t=1}^n \sum_{r=2^{t-1}+1}^{2^t-1} (2^n - r + 1) \lceil \log_2 r \rceil. \end{aligned}$$

It can also be shown through simple algebraic operations that

$$\begin{aligned} & \sum_{t=1}^n \sum_{r=2^{t-1}+1}^{2^t-1} (2^n - r + 1) \lceil \log_2 r \rceil = (2^n + 1) \frac{n(n+1)}{2} \\ & - \frac{3}{2} \left( \frac{(3n-1)4^n + 1}{9} - (n-1)2^n - 1 \right) \\ & = \frac{11 + 3(n^2 - 2^{n+1}) + 3n(n+3)2^n - (3n-1)2^{2n}}{6}. \end{aligned}$$

□

The following theorem states that the minimum average code length is met by the built-in encoding scheme inside the procedure of Theorem 5.3.

**Theorem 5.6** *The algorithm introduced by Theorem 5.3 assigns codes to  $(n, n)_{\mathcal{PS}}$ -algorithms with an average length of  $\left\lceil \log_2 \left( \prod_{i=0}^{2^n-1} (2^n - i)^{i+1} \right) \right\rceil$ .*

**Table 5.4** A  $(2, 2)_{\mathcal{PS}}$ -algorithm encoded as 100011111

Function code	Plain text	Cipher text
00	00	11
00	01	10
00	10	01
00	11	00
01	00	11
01	01	10
01	10	00
01	11	01
10	00	11
10	01	01
10	10	10
10	11	00
11	00	11
11	01	01
11	10	00
11	11	10

**Proof** The algorithm assigns 0 to the first created  $(n, n)_{\mathcal{PS}}$ -algorithm, and thus, the total number of assigned codes is equal to  $\prod_{i=0}^{2^n-1} (2^n - i)^{i+1} - 1$ , so we can represent them by binary sequences of length  $\lceil \log_2 \left( \prod_{i=0}^{2^n-1} (2^n - i)^{i+1} \right) \rceil$ . □

$(n, n)_{\mathcal{PS}}$ -algorithms can be considered as the collection of  $2^n$  reversible  $(n, n)$ -functions with satisfy some fixed conditions. Thus, we can use other permutation encoding methods. Encoding permutations has been research focus during recent decades [631, 632]. Each of the proposed methods may have its own advantages and disadvantages. Some of them are purely numeric [631] and some are not [632]. But our encoding scheme was proven to assign codes with the minimum average lengths. Table 5.4 shows a sample  $(2, 2)_{\mathcal{PS}}$ -algorithm encoded by this scheme.

### 5.2.2.7 Decryption Algorithms

So far, we have only discussed encryption algorithms. Another issue to deal with here is the design of decryption algorithms. Since every  $(n, n)_{\mathcal{PS}}$ -algorithm consists as the collection of  $2^n$  reversible  $(n, n)$ -functions with satisfy some fixed conditions, the decryption algorithm can be obtained by reversing individual  $(n, n)$ -function in the encryption algorithm. Table 5.5 shows a pair of perfectly secure encryption/decryption algorithms.

**Table 5.5** A perfectly secure encryption algorithm along with the corresponding decryption algorithm

Encryption			Decryption		
Key	$\mathcal{P}$	$\mathcal{C}$	Key	$\mathcal{C}$	$\mathcal{P}$
00	00	00	00	00	00
	01	01		01	01
	10	11		10	11
	11	10		11	10
01	00	01	01	00	10
	01	10		01	00
	10	00		10	01
	11	11		11	11
10	00	10	10	00	11
	01	11		01	10
	10	01		10	00
	11	00		11	01
11	00	11	11	00	01
	01	00		01	11
	10	10		10	10
	11	01		11	00

**Fig. 5.3** The Latin squares corresponding to the encryption and decryption algorithms in Table 5.1

Encryption				Decryption			
00	01	11	10	00	01	11	10
01	10	00	11	10	00	01	11
10	11	01	00	11	00	00	01
11	00	10	01	01	11	10	00

### 5.2.2.8 Mapping to Latin Squares

According to the above discussions, each truth table, representing a  $(n, n)_{\mathcal{PS}}$ -algorithm clearly consists of  $2^n \cdot 2^n = 2^{2n}$  lines. For each  $(n, n)_{\mathcal{PS}}$ -algorithm  $A$ , the set  $\mathcal{L}_A$  of lines divided into  $2^n$  chunks  $\mathcal{L}_A(0), \mathcal{L}_A(1), \dots, \mathcal{L}_A(2^n - 1)$  each containing  $2^n$  consequent individual lines, such that the following conditions hold.

- $\forall i \in \{0, 1, \dots, 2^n - 1\} : \{\mathcal{L}_A(i)(j) | j \in \{0, 1, \dots, 2^n - 1\}\} = \{0, 1, \dots, 2^n - 1\}$ ,
- $\forall j \in \{0, 1, \dots, 2^n - 1\} : \{\mathcal{L}_A(i)(j) | i \in \{0, 1, \dots, 2^n - 1\}\} = \{0, 1, \dots, 2^n - 1\}$ ,

where  $\mathcal{L}_A(i)(j)$  is the decimal representation of the  $j$ th entry in the  $i$ th chunk.

The above criteria clearly define a Latin square of order  $n$ . This maps perfectly secure algorithms to Latin squares, and the reader can easily verify that the mapping is one-to-one.

For example, the Latin squares corresponding to the truth tables of the encryption and decryption algorithms in Table 5.1 are shown in Fig. 5.3.

### 5.2.2.9 Secret Algorithm Perfect Secrecy

The following theorem forms the basis of our secret algorithm perfectly secure cryptographic scheme.

**Theorem 5.7** *Consider a cryptography scheme in which one among all possible  $(n, n)_{\mathcal{R}}$ -functions can be selected to transform the plain text to cipher text according to a given function code. This cryptography scheme will be perfectly secure.*

**Proof** Since  $(n, n)_{\mathcal{R}}$ -functions are permutations and the cryptography scheme selects among all permutations of  $2^n$  possible cipher text values, the number of permutations converting every given plain text to every given cipher text will be the same and equal to  $(2^n - 1)!$ . Thus, such a system will be perfectly-secure.  $\square$

On the basis of the above theorem, we define a secret algorithm cryptography scheme with plain text length equal to  $n$  as the collection of all possible  $(n, n)_{\mathcal{R}}$ -functions, one among which is selected using a secret function code. If  $n = 2$ , such a collection can be imagine as shown in Table 5.6.

In a cryptography scheme explained in the above theorem, we can consider every individual  $(n, n)$ -function as a distinct encryption algorithm. Moreover, the function code can be considered as the algorithm code. In fact, such a system can depend on a secret algorithm code instead of a key for its confidentiality.

A secret algorithm perfectly secure cryptography scheme has a second important advantage to a traditional cryptography with a  $n$ -bit key and  $n$ -bit plain/cipher texts in addition to perfect secrecy. In such a scheme, the malicious third party has to test (at most)  $2^n!$  instead of  $2^n$  key values. This requires much more time and more complex hardware/software.

## 5.3 Concluding Remarks: The Proposed Approach and IoT

Our work in this chapter is in fact one step toward both perfectly secure and random algorithm cryptography in resource-constrained IoT-based applications. We first established a connection between perfectly secure encryption/decryption algorithms and  $n$ -resilient Boolean functions. Then, we solved the problem of exhaustively creating, counting, and encoding all theoretically possible perfectly secure cryptographic algorithms. Next, we developed a system model for cryptosystems that depend on secret algorithms instead of or in addition to secret keys for perfect secrecy. The system model makes it possible to discuss the advantages, disadvantage, challenges, and requirements of secret algorithm perfectly secure cryptosystems. This research work can be continued by research on hardware/software implementation of the secret algorithm perfectly secure cryptosystems. Researchers can also continue our work by presenting more efficient encoding schemes.

Our proposed approach is especially useful for IoT due to the following reasons.

**Table 5.6** Codes assigned to all possible  $(2, 2)_{\mathcal{R}}$ -functions

Algorithm	$\mathcal{P}$	$\mathcal{C}$	Algorithm	$\mathcal{P}$	$\mathcal{C}$	Algorithm	$\mathcal{P}$	$\mathcal{C}$
00000	00	00	01000	00	01	10000	00	10
	01	01		01	10		01	11
	10	10		10	00		10	00
	11	11		11	11		11	01
00001	00	00	01001	00	01	10001	00	10
	01	01		01	10		01	11
	10	11		10	11		10	01
	11	10		11	00		11	00
00010	00	00	01010	00	01	10010	00	11
	01	10		01	11		01	00
	10	01		10	00		10	01
	11	11		11	10		11	10
00011	00	00	01011	00	01	10011	00	11
	01	10		01	11		01	00
	10	11		10	10		10	10
	11	01		11	00		11	01
00100	00	00	01100	00	10	10100	00	11
	01	11		01	00		01	01
	10	01		10	01		10	00
	11	10		11	11		11	10
00101	00	00	01101	00	10	10101	00	11
	01	11		01	00		01	01
	10	10		10	11		10	10
	11	01		11	01		11	00
00110	00	01	01110	00	10	10110	00	11
	01	00		01	01		01	10
	10	10		10	00		10	00
	11	11		11	11		11	01
00111	00	01	01111	00	10	10111	00	11
	01	00		01	01		01	10
	10	11		10	11		10	01
	11	10		11	00		11	00

- We have demonstrated (earlier in this book) the efficiency of information-theoretic cryptography in real-time and embedded IoT cryptography.
- We have already shown the efficiency of Latin squares in IoT cryptography.
- We have discussed the efficiency of Boolean cryptography in real-time and embedded IoT cryptography.
- The secret algorithm cryptography makes it possible to design robust cryptographic schemes even with shorter word length, which makes it a good choice for cryptography in real-time and resource-constrained environments such as IoT.

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